Simulating Dark Matter Self-Interactions

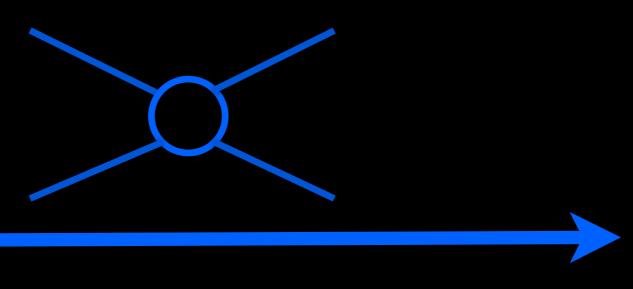
Miguel Rocha - UC Irvine

Harvard Self-Interacting Dark Matter Workshop
08/06/2013



Outline

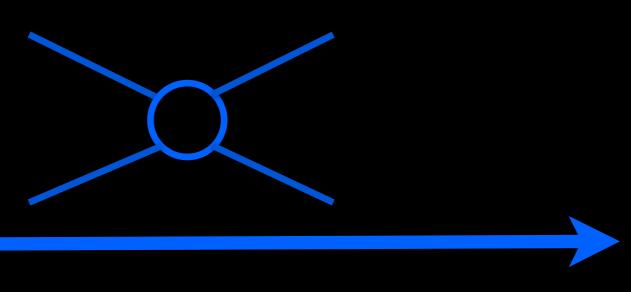
- Implementing DM self-iteractions A new self-consistent algorithm
- Results from cosmological simulations Halo densities, shapes and substructure
- Work in progress and future goals Expand simulation sample, merging clusters, etc ...



large mean free paths

Collisionality

short mean free paths



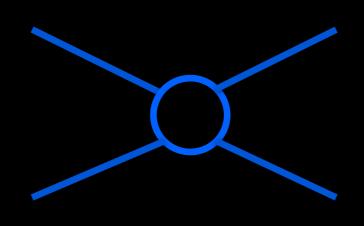
large mean free paths

Collisionality

short mean free paths

Vlavsov equation solved with

collisionless N-body



large mean free paths

|

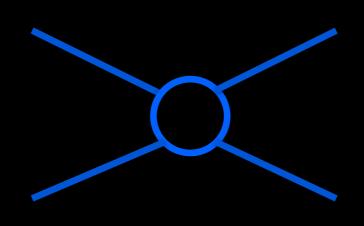
Vlavsov equation solved with collisionless N-body

Collisionality

short mean free paths



Fluid equations solved with hydro methods



large mean free paths

J

Vlavsov equation solved with collisionless N-body

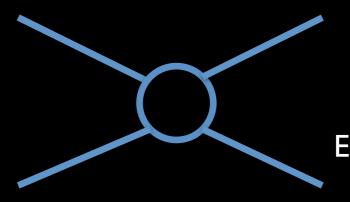
Collisionality

Spergerl & Steinhardt 2000

short mean free paths

Fluid equations solved with hydro methods

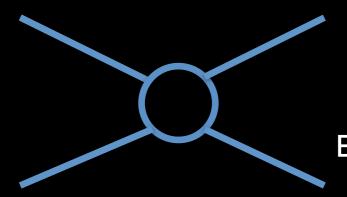




Spergerl & Steinhardt 2000
$$\Gamma = \rho \left(\frac{\sigma}{m}\right) v_{rel}$$
 Elastic - Velocity Independent - Isotropic

$$P_i = \rho_i \left(\frac{\sigma}{m}\right) V_i \Delta t$$

Burkert 2000, Kochaneck & White 2000, Yoshida et al. 2000b



Elastic - Velocity Independent - Isotropic

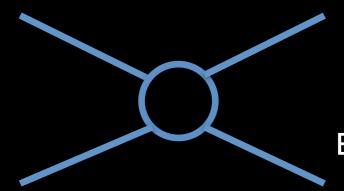
Spergerl & Steinhardt 2000
$$\Gamma = \rho \left(\frac{\sigma}{m}\right) v_{rel}$$
c - Velocity Independent - Isotropic

$$P_i = \rho_i \left(\frac{\sigma}{m}\right) V_i \Delta t$$

Burkert 2000, Kochaneck & White 2000, Yoshida et al. 2000b

$$P_i = \sum_{i} mW(|\hat{\mathbf{x}}_i - \hat{\mathbf{x}}_j|, h_j) \left(\frac{\sigma}{m}\right) |\hat{\mathbf{v}}_i - \hat{\mathbf{v}}_j| \Delta t$$

Koda & Shapiro 2011, Vogelsberger et al. 2012



Elastic - Velocity Independent - Isotropic

Spergerl & Steinhardt 2000
$$\Gamma = \rho \left(\frac{\sigma}{m}\right) v_{rel}$$
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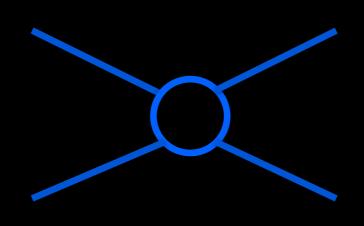
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Burkert 2000, Kochaneck & White 2000, Yoshida et al. 2000b

$$P_i = \sum_{j} mW(|\hat{\mathbf{x}}_i - \hat{\mathbf{x}}_j|, h_j) \left(\frac{\sigma}{m}\right) |\hat{\mathbf{v}}_i - \hat{\mathbf{v}}_j| \Delta t$$

Koda & Shapiro 2011, Vogelsberger et al. 2012

$$P(i|j) \neq P(j|i)$$



large mean free paths

J

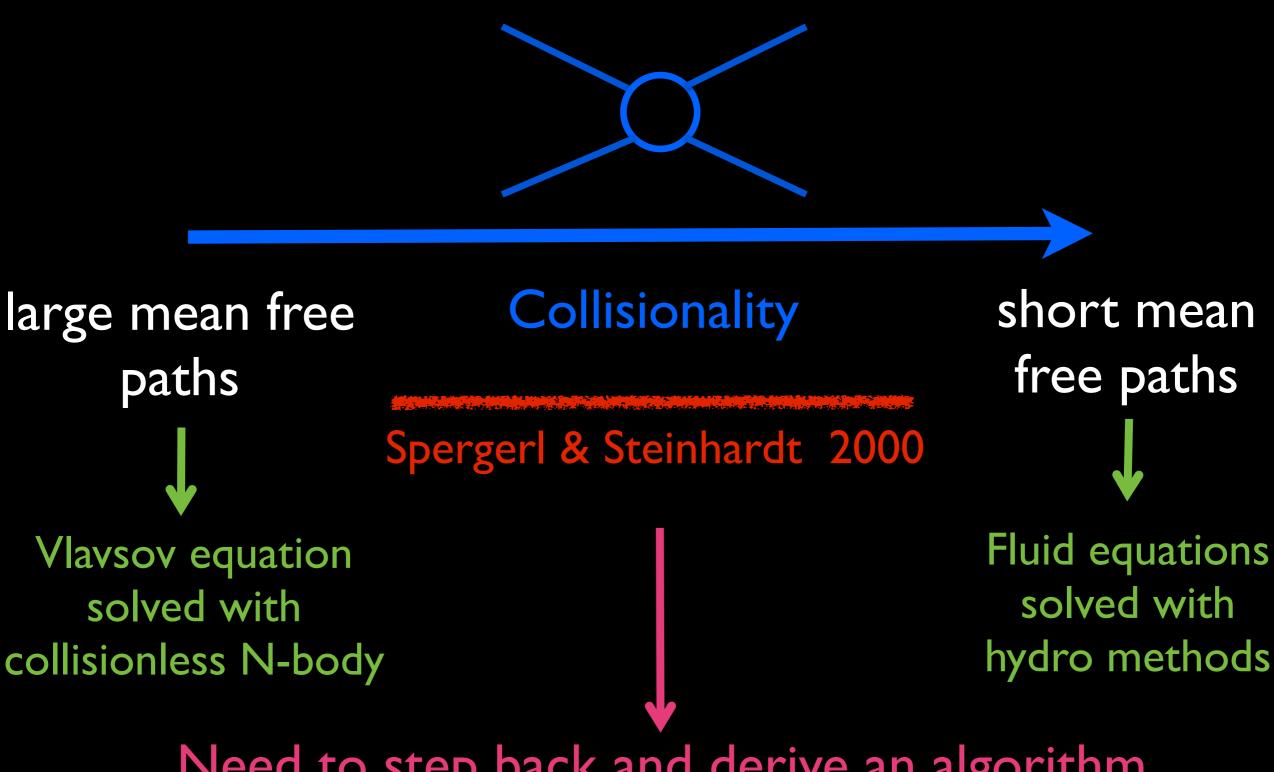
Vlavsov equation solved with collisionless N-body

Collisionality

Spergerl & Steinhardt 2000

short mean free paths

Fluid equations solved with hydro methods



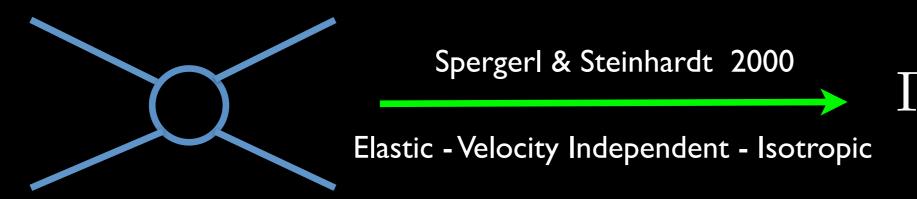
Need to step back and derive an algorithm from the Boltzmann Equation



phase-space evolution given by the Boltzmann Eq. with a hard-sphere collision operator

$$\frac{Df(\mathbf{x}, \mathbf{v}, t)}{Dt} = \Gamma[f, \sigma]$$

$$= \int d^3 \mathbf{v}_1 \int d\Omega \frac{d\sigma}{d\Omega} |\mathbf{v} - \mathbf{v}_1| \left[f(\mathbf{x}, \mathbf{v}', t) f(\mathbf{x}, \mathbf{v}'_1, t) - f(\mathbf{x}, \mathbf{v}, t) f(\mathbf{x}, \mathbf{v}_1, t) \right]$$



$$\Gamma = \rho \left(\frac{\sigma}{m}\right) v_{rel}$$

phase-space evolution given by the Boltzmann Eq. with a hard-sphere collision operator

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$$\hat{f}(\mathbf{x}, \mathbf{v}, t) = \sum_{i} (M_i/m) W(|\mathbf{x} - \mathbf{x}_i|; h_i) \delta^3(\mathbf{v} - \mathbf{v}_i)$$

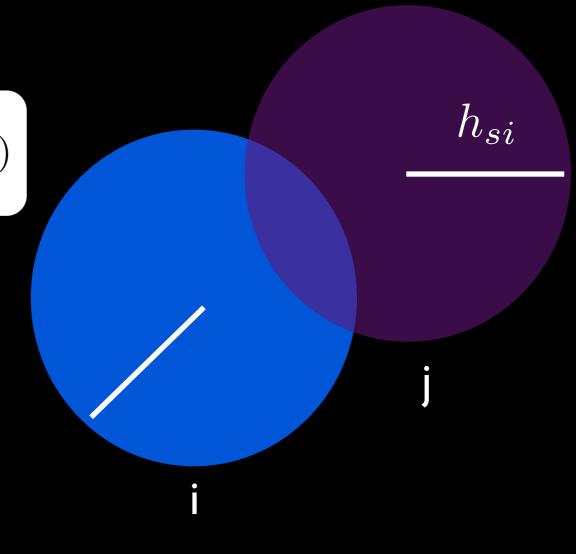
Consistent Pair-Wise Probability

$$\Gamma(i|j) = (\sigma/m)m_{\rm p}|\mathbf{v}_i - \mathbf{v}_j|g_{ji}$$

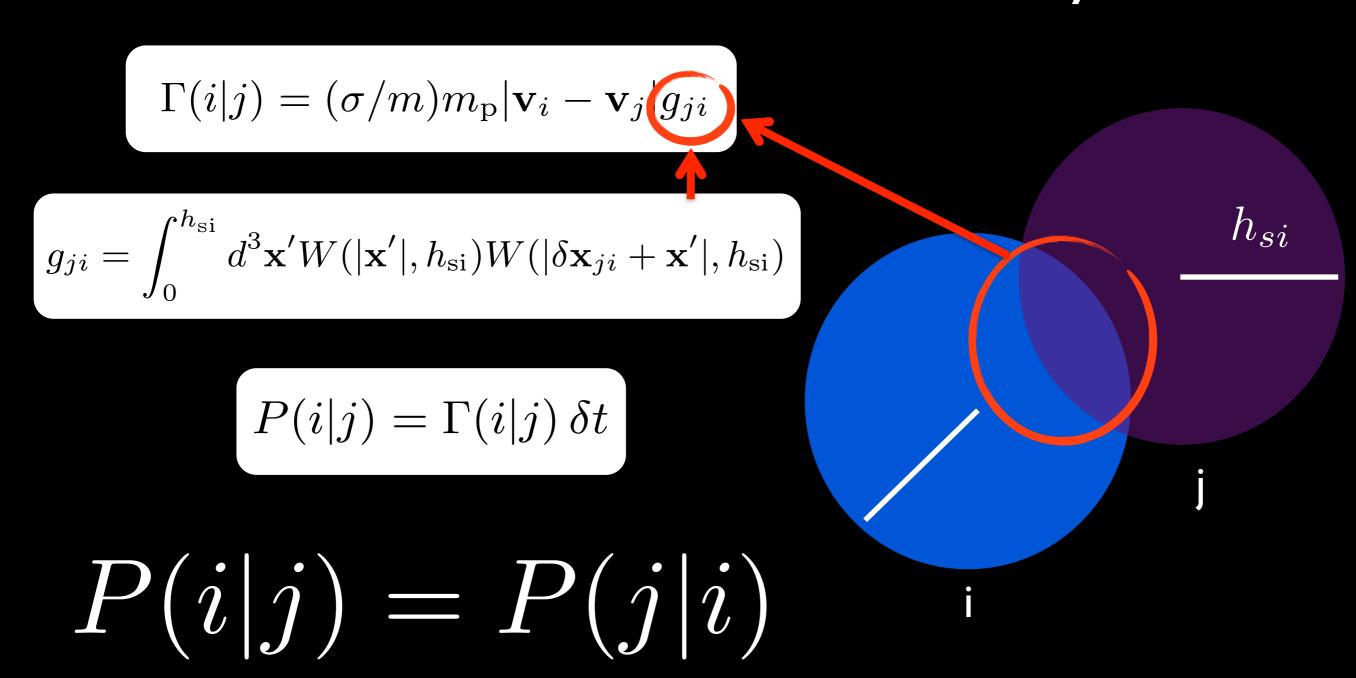
$$g_{ji} = \int_0^{h_{si}} d^3 \mathbf{x}' W(|\mathbf{x}'|, h_{si}) W(|\delta \mathbf{x}_{ji} + \mathbf{x}'|, h_{si})$$

$$P(i|j) = \Gamma(i|j) \,\delta t$$

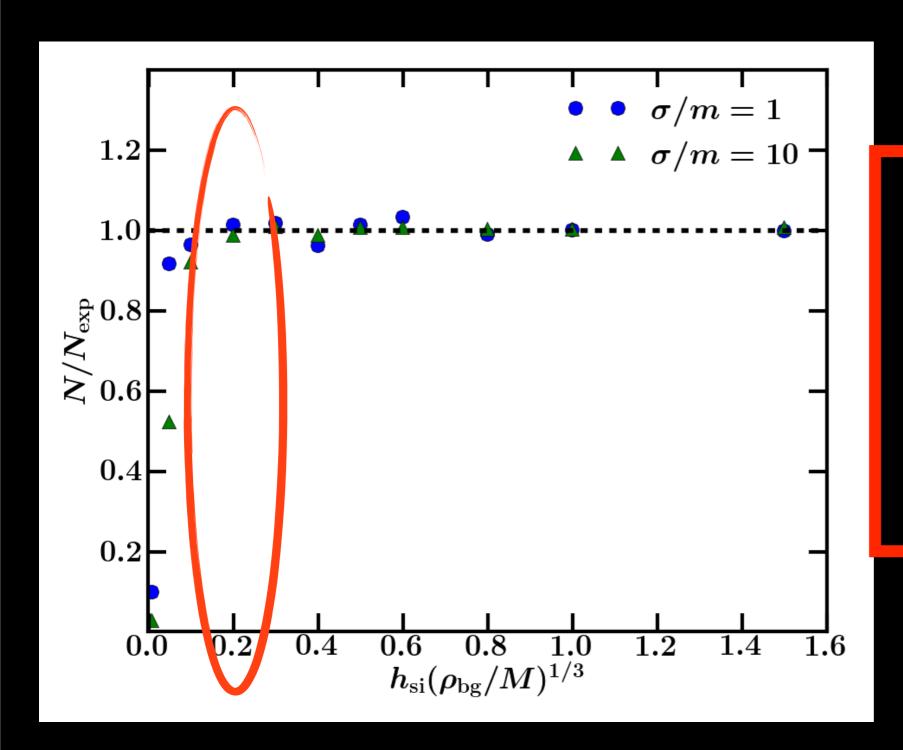
$$P(i|j) = P(j|i)$$



Consistent Pair-Wise Probability



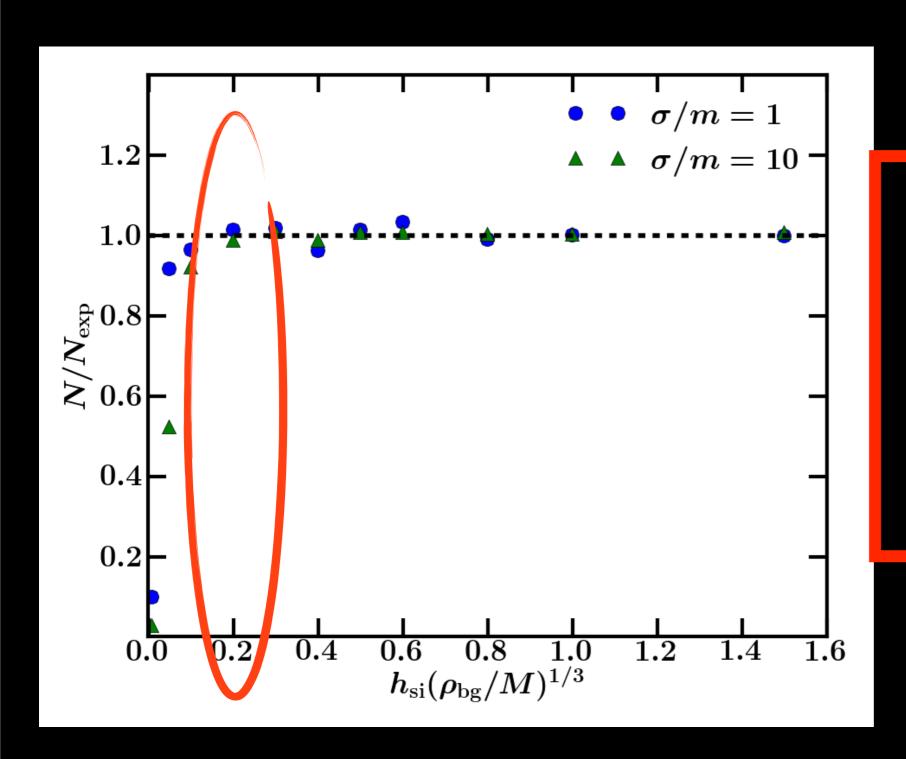
Wind Tunnel Test



Interaction rate converges to the expected value when h_{si} >0.2* (the interparticle separation)

Rocha et al. 2013 Peter et al. 2013

Wind Tunnel Test

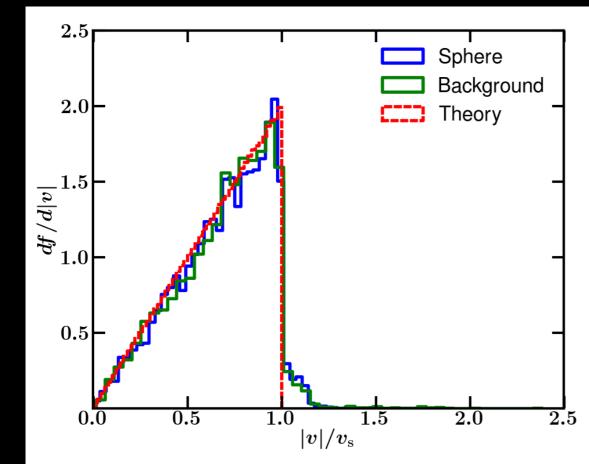


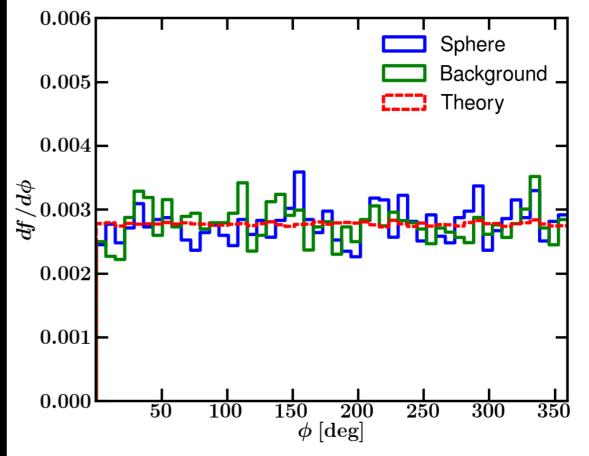


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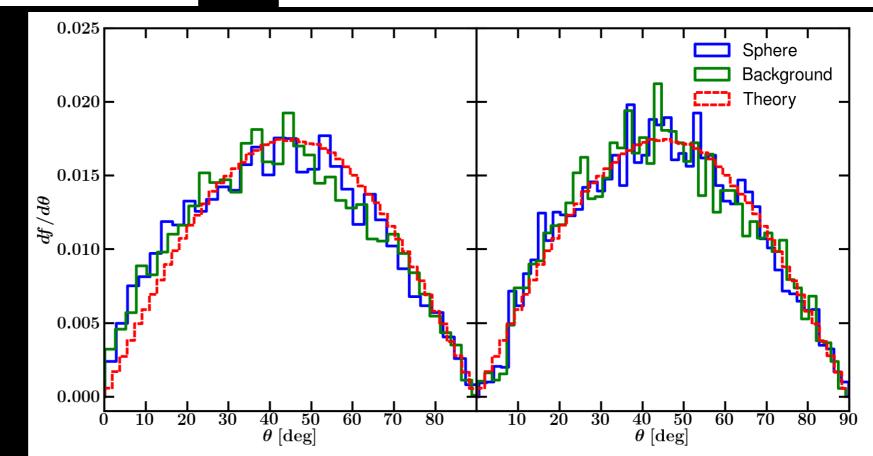
Wind Tunnel Test





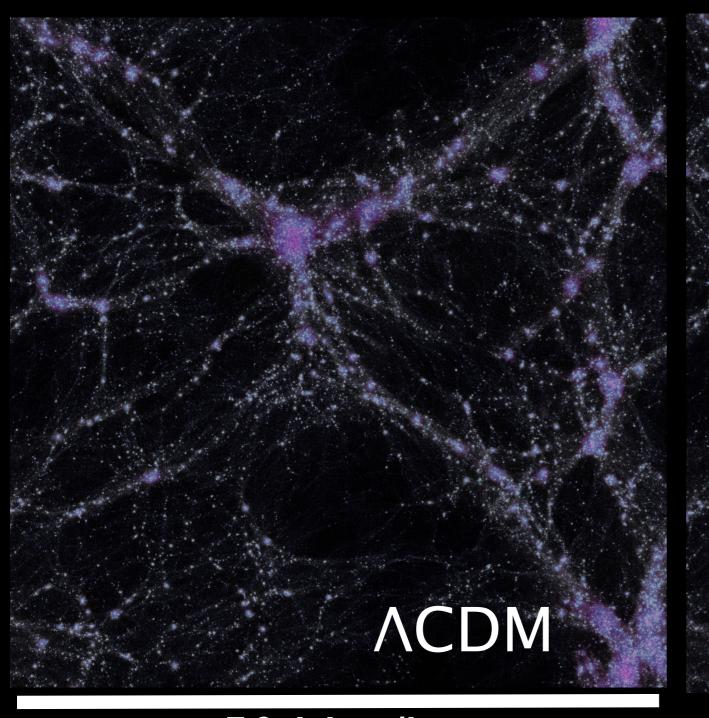


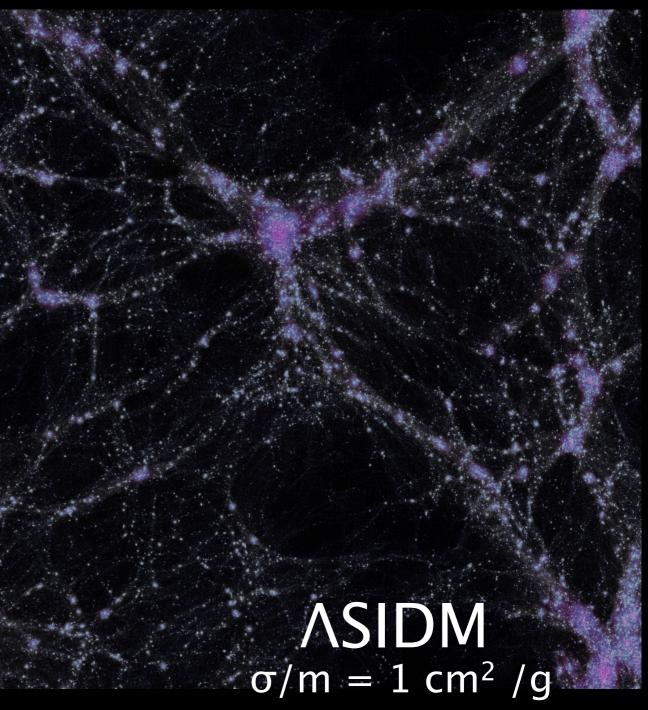
Correct post-scatter kinematics



Results from cosmological simulations - Halo densities, shapes & substructure

Identical large-scale structure





50 Mpc/h

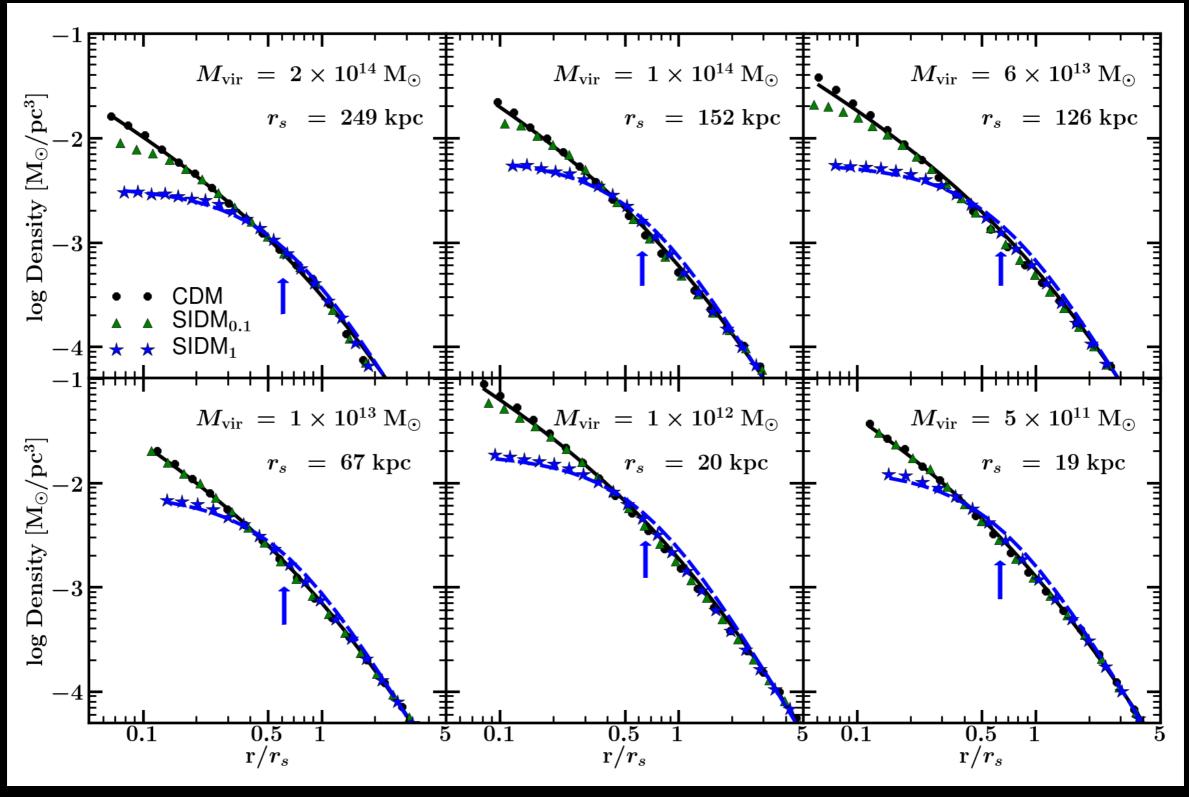
Results from cosmological simulations - Halo densities, shapes & substructure

Lower central phase-space density in SIDM halos

 Λ CDM

200 Kpc/h

 Λ SIDM $\sigma/m = 1 \text{ cm}^2/g$



Radius/rs

 $\sigma/m = 1$ $\sigma/m = 0.1$

Artificial 2-body scattering when $~t_{relax} \sim \frac{1}{H_o}$

Power et al. 2003

Artificial 2-body scattering when $~t_{relax} \sim \frac{1}{H_o}$

Power et al. 2003

Need ~ 10^6-10^7 particles within the virial radius to resolve the cores of $\sigma/m = 1-0.1$ cm²/g halos

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$$t_{relax} \propto \frac{N_{enc}}{\sqrt{\tilde{
ho}}} = \frac{V_{enc}}{m_p} \sqrt{\tilde{
ho}}$$

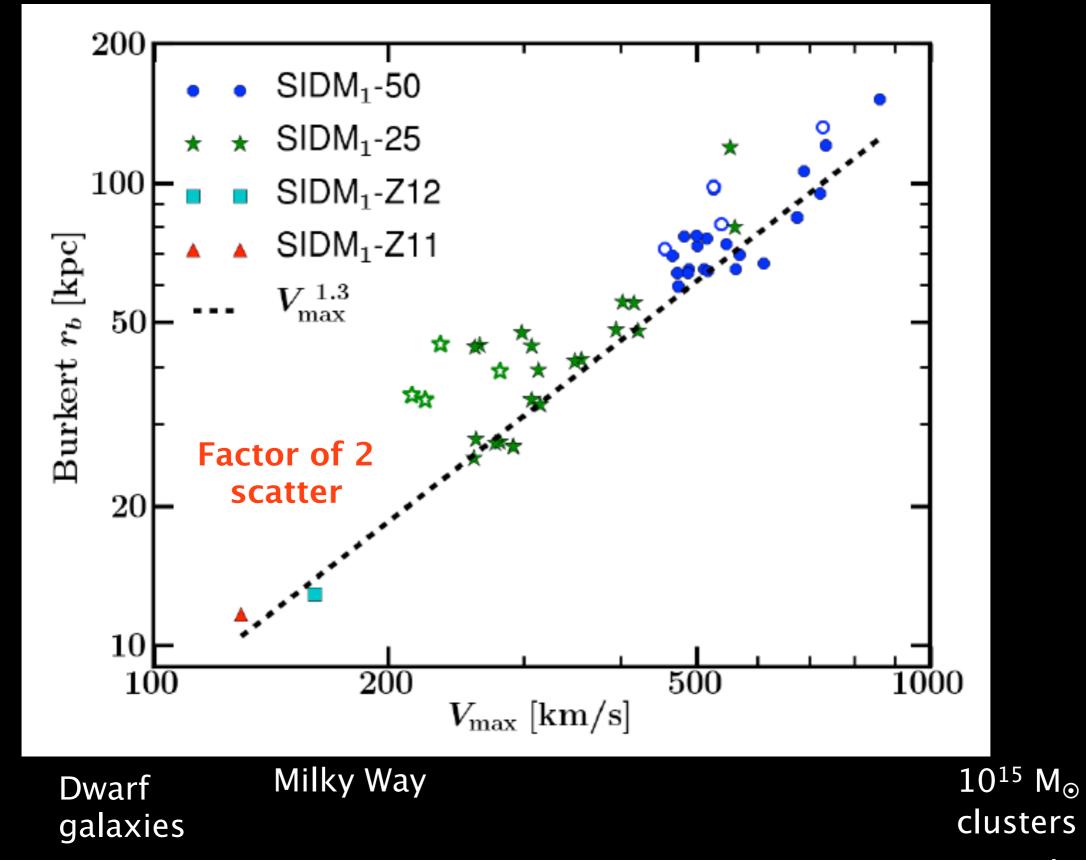
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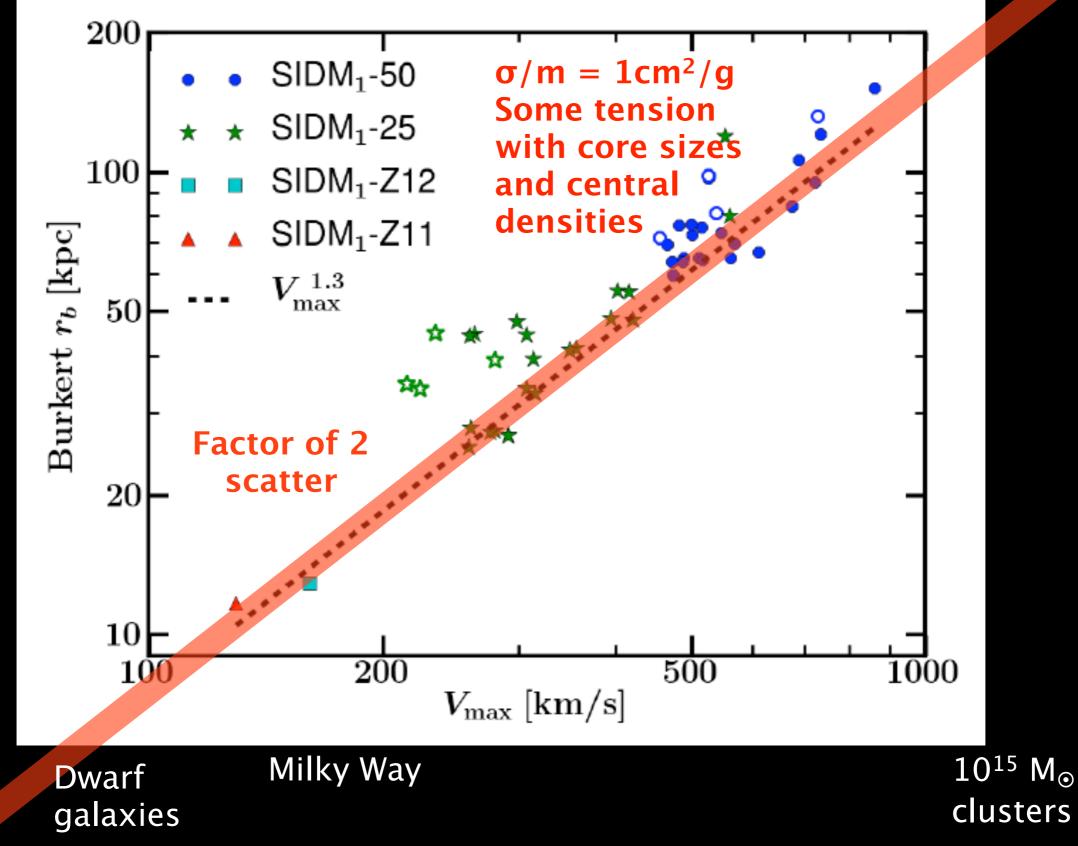
$$t_{relax} \propto \frac{N_{enc}}{\sqrt{\tilde{
ho}}} = \frac{V_{enc}}{m_p} \sqrt{\tilde{
ho}}$$

For a fixed volume and mass resolution cored halos are harder to resolve!!

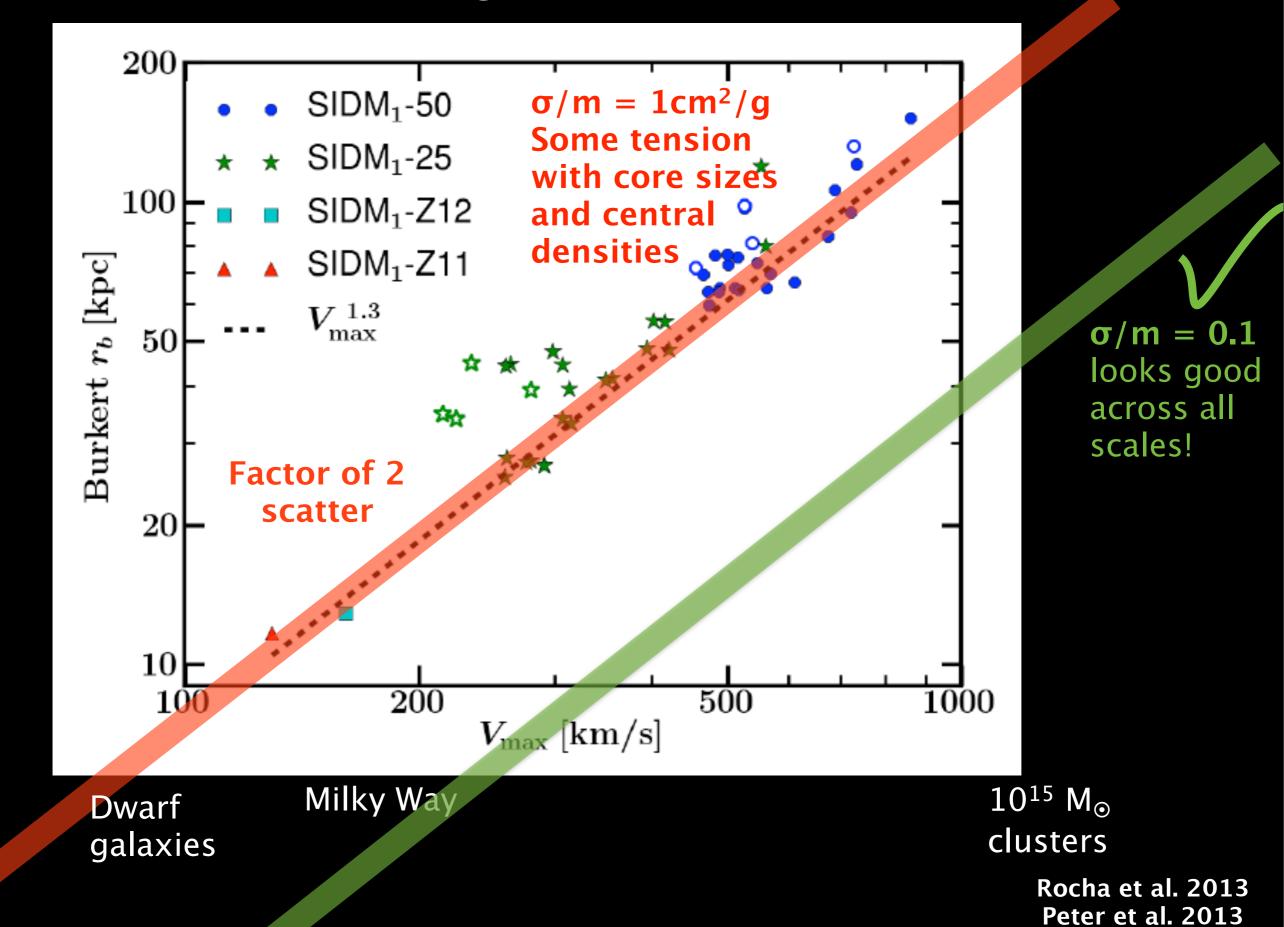


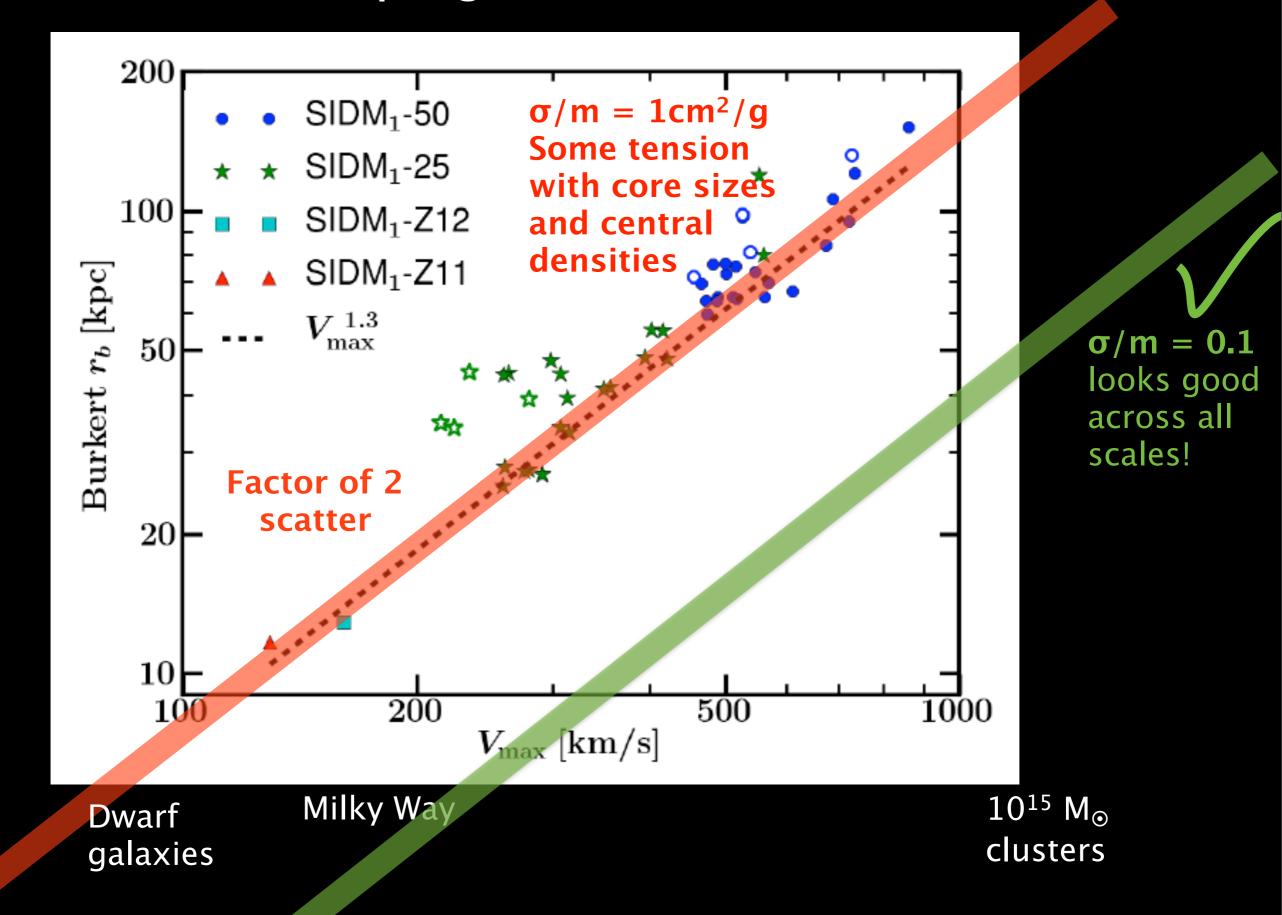
Friday, August 9, 13

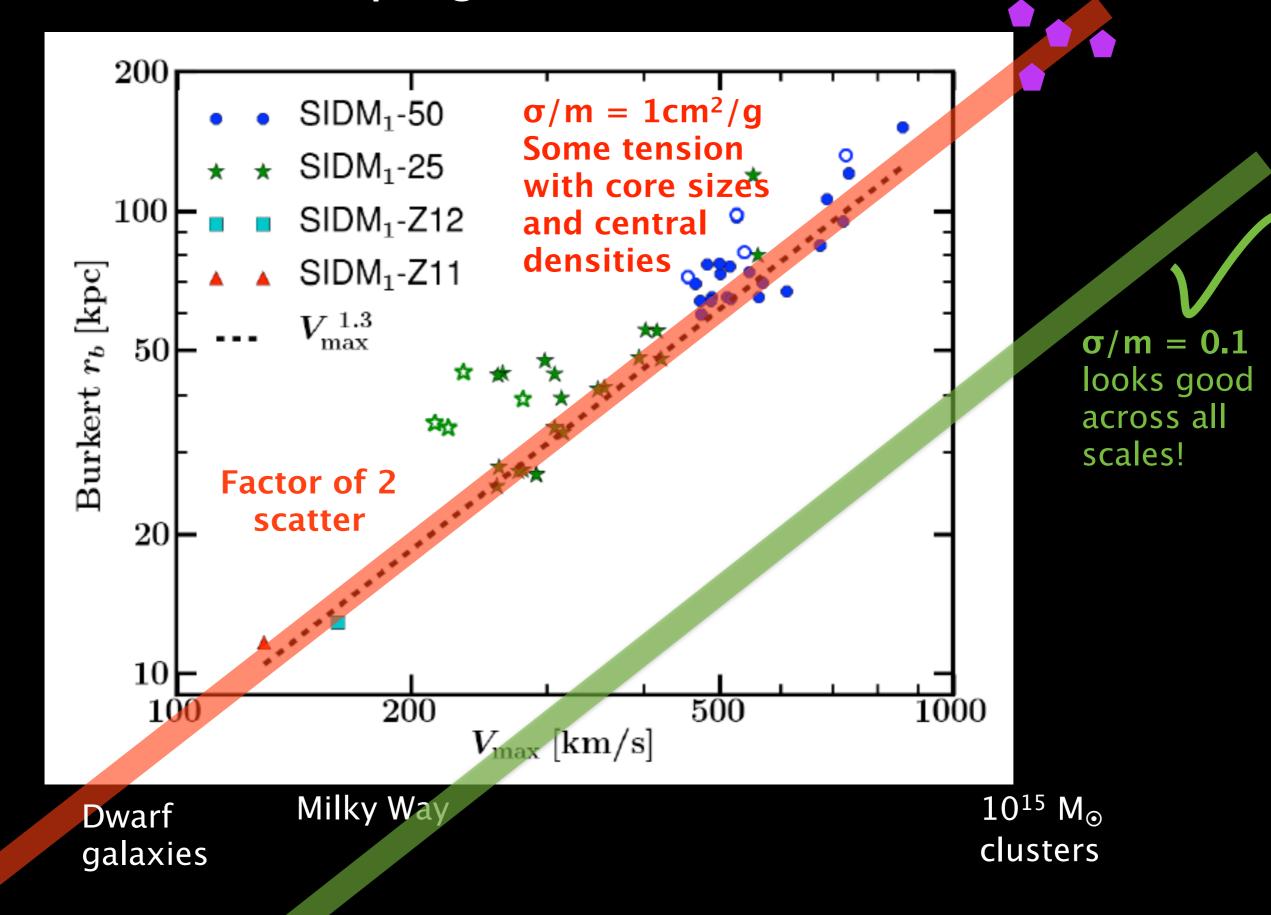
Rocha et al. 2013 Peter et al. 2013

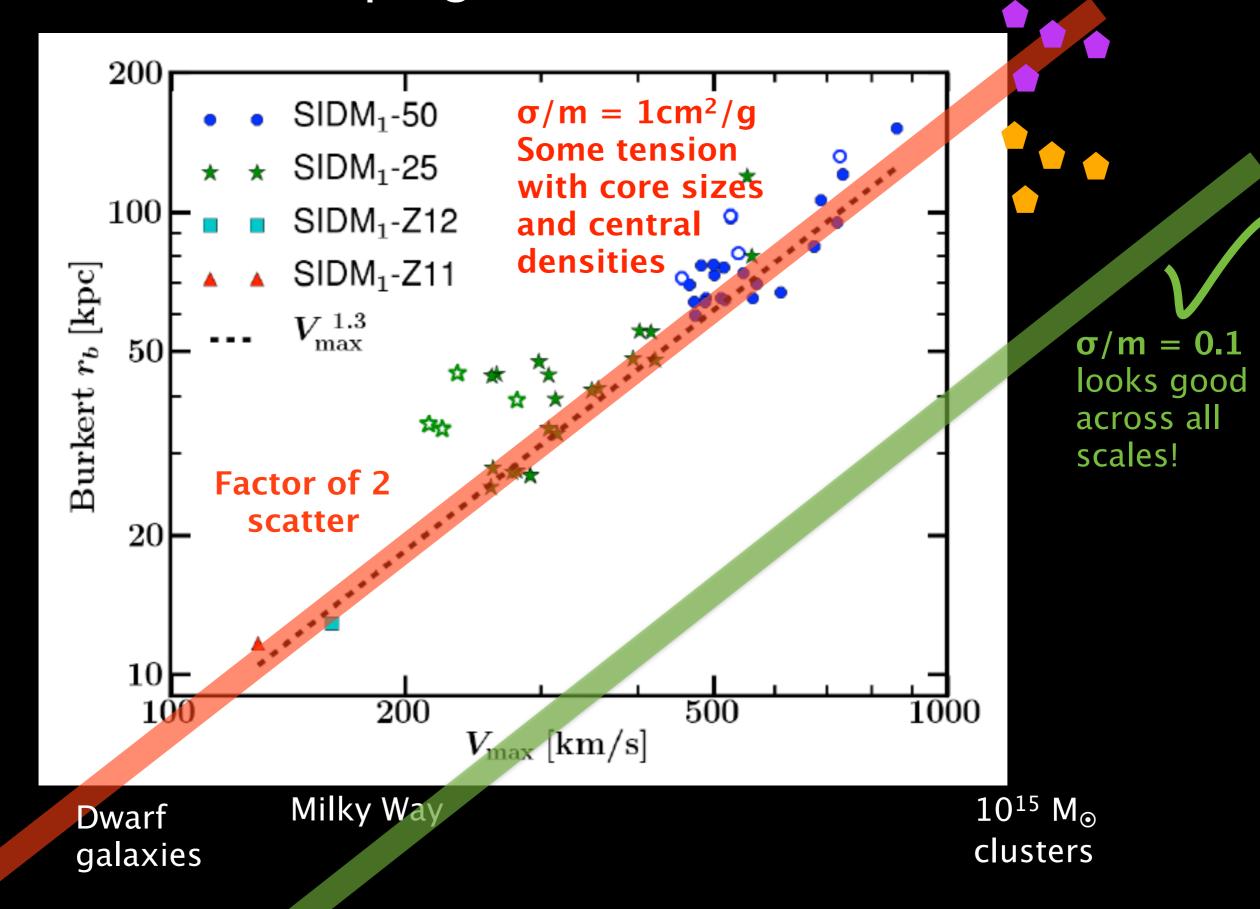


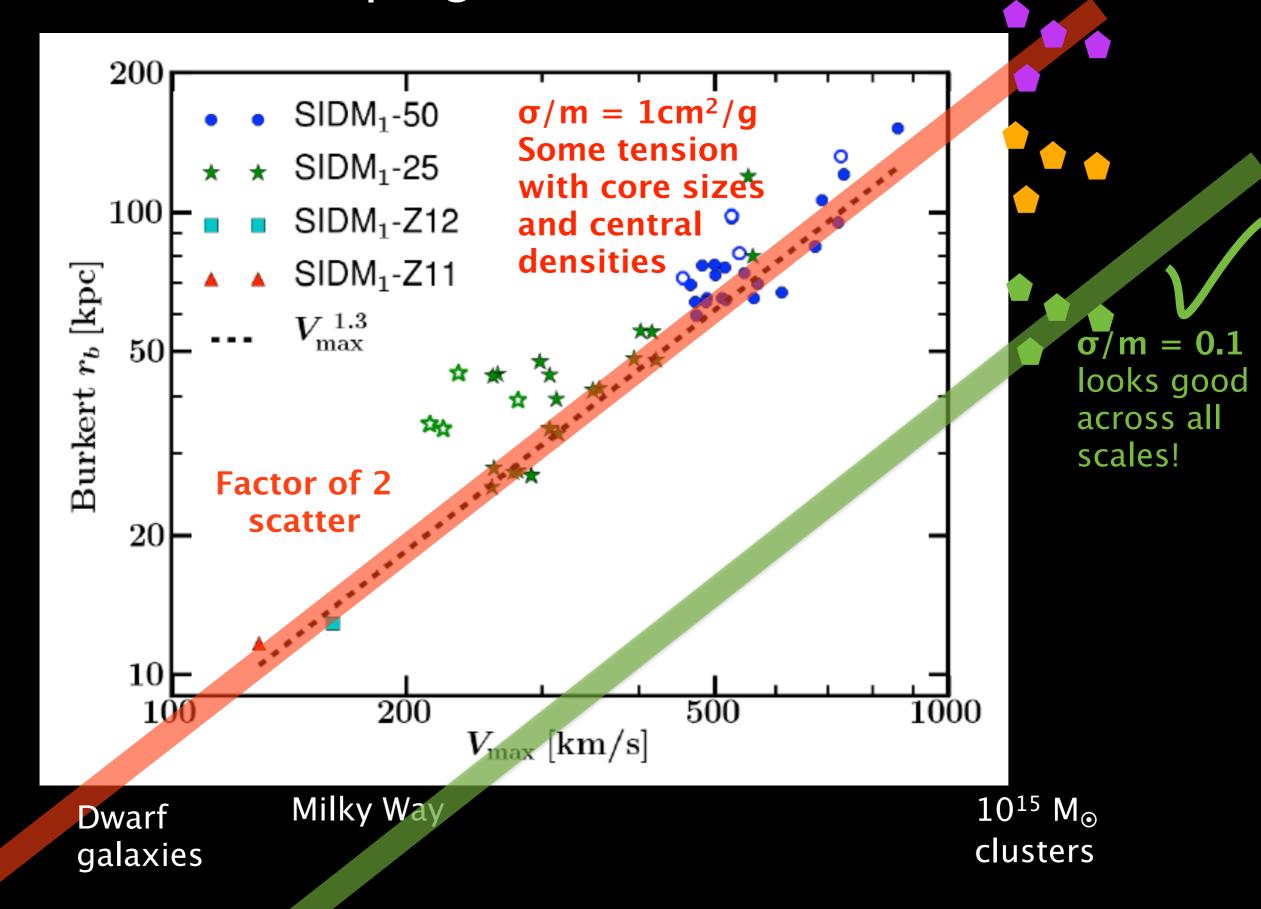
Rocha et al. 2013 Peter et al. 2013

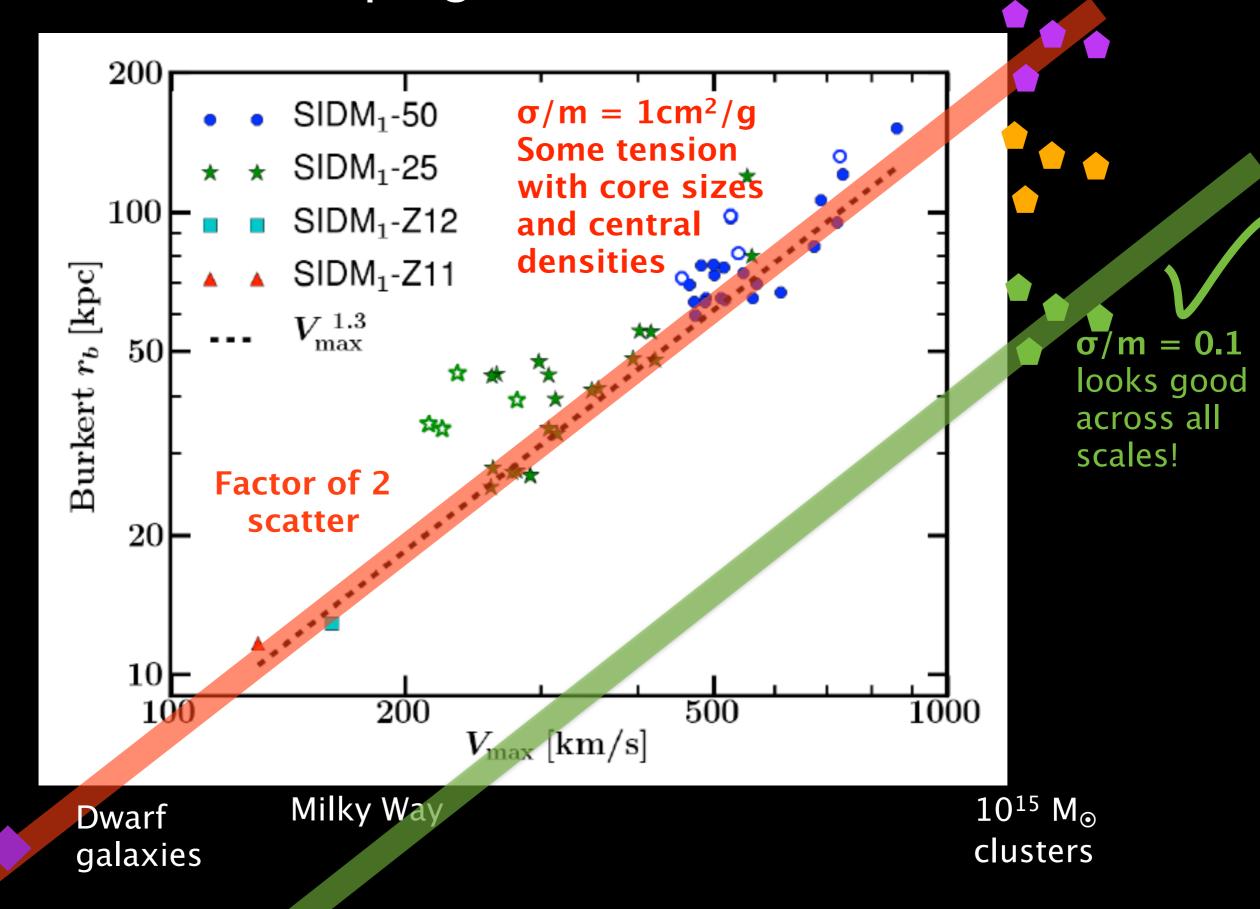


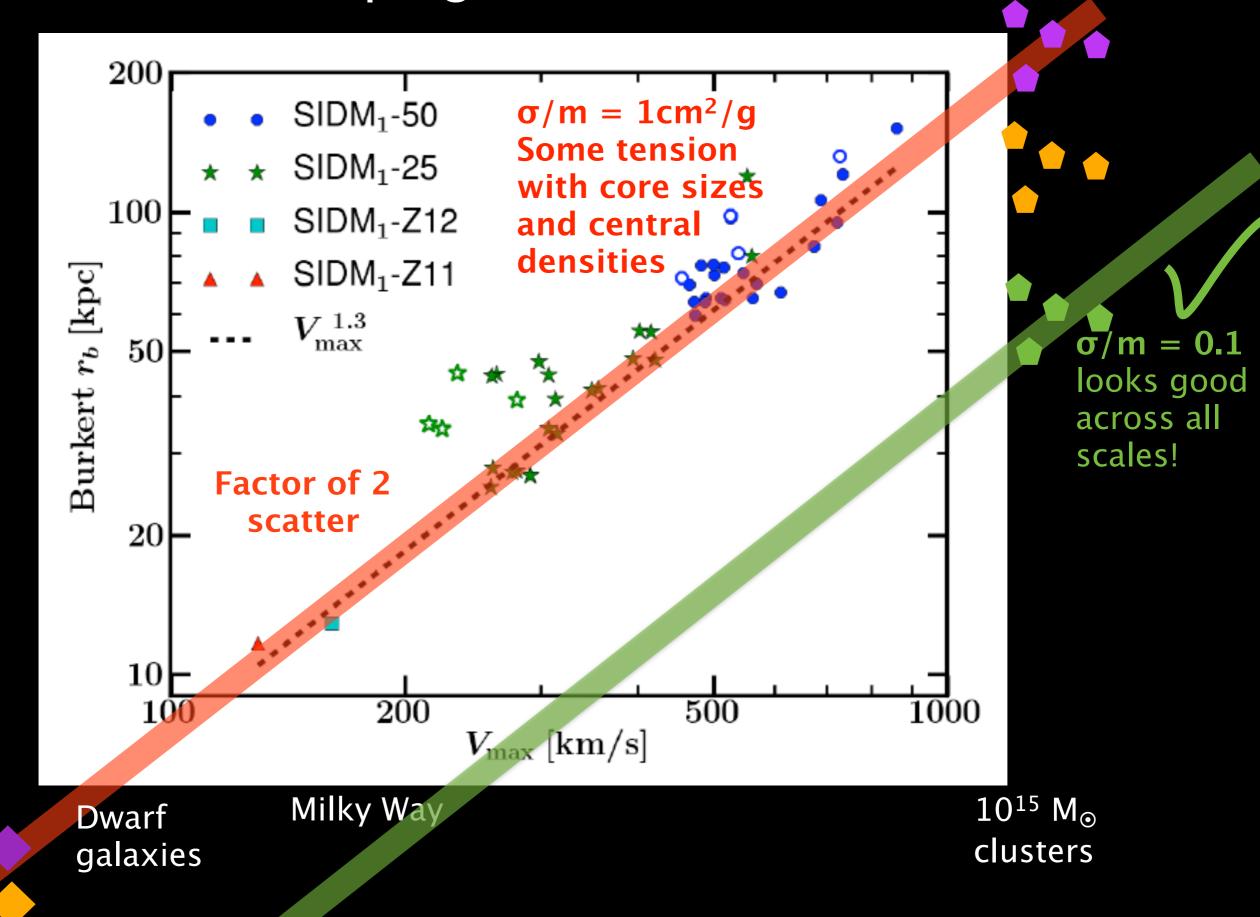


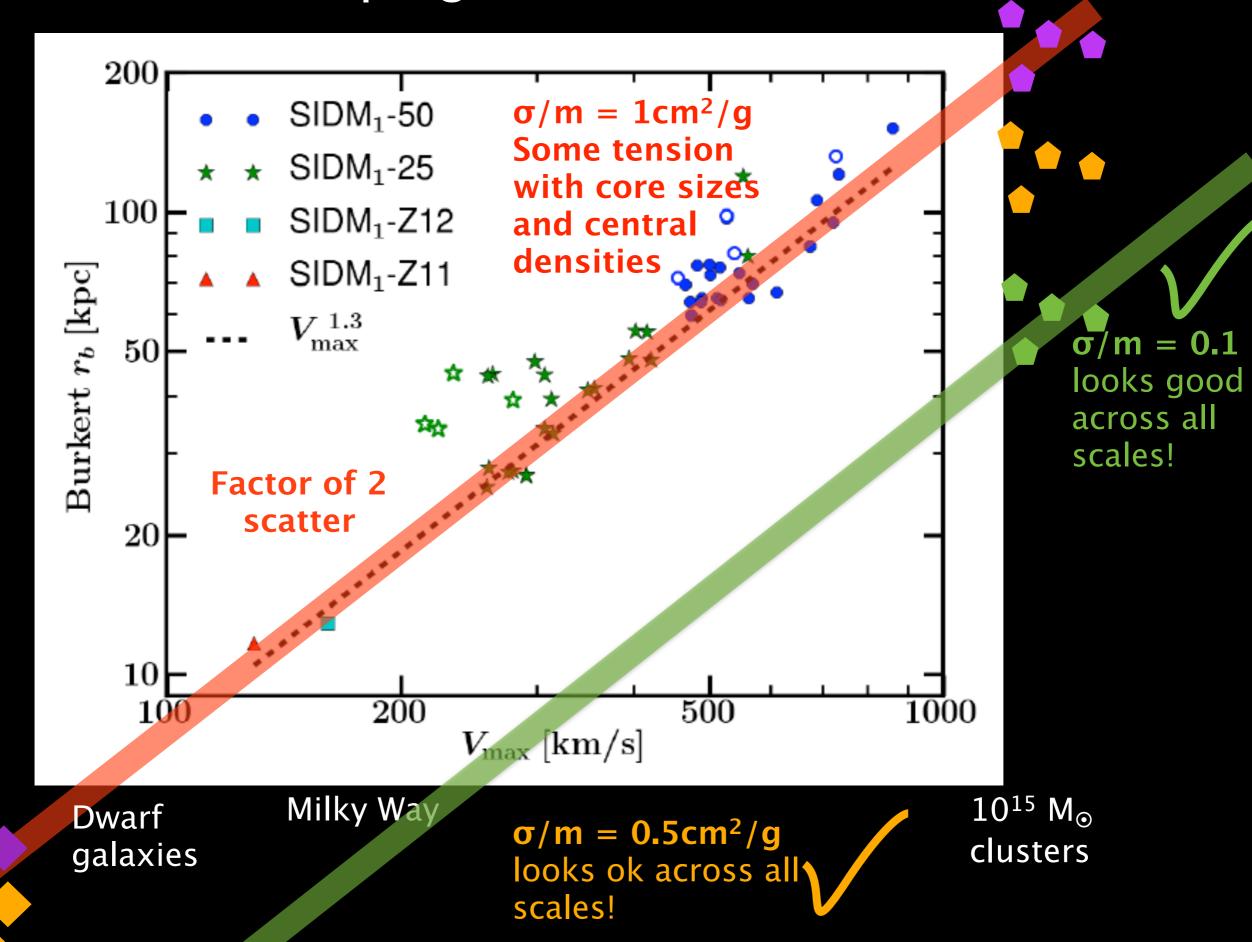


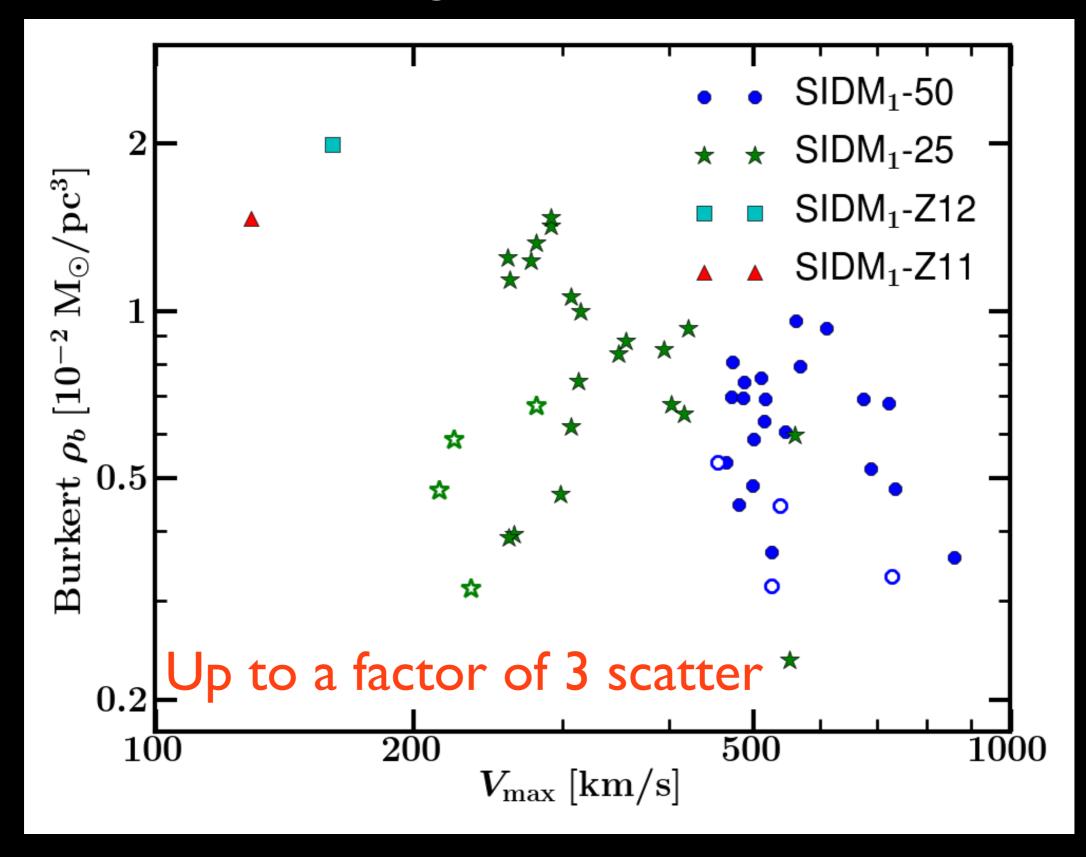






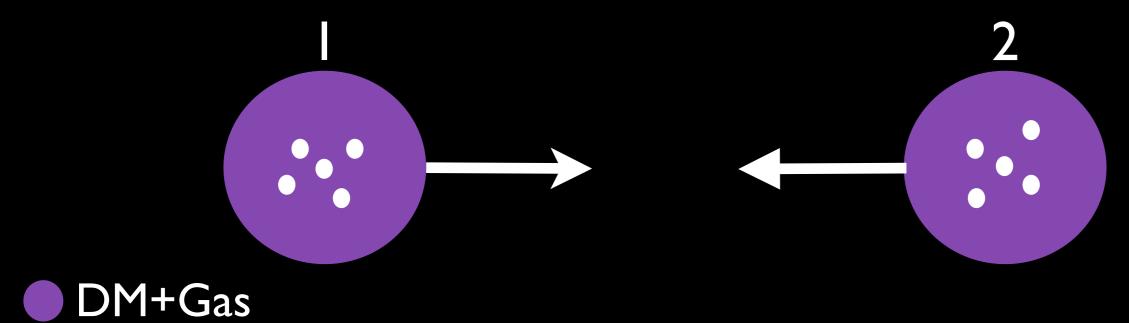




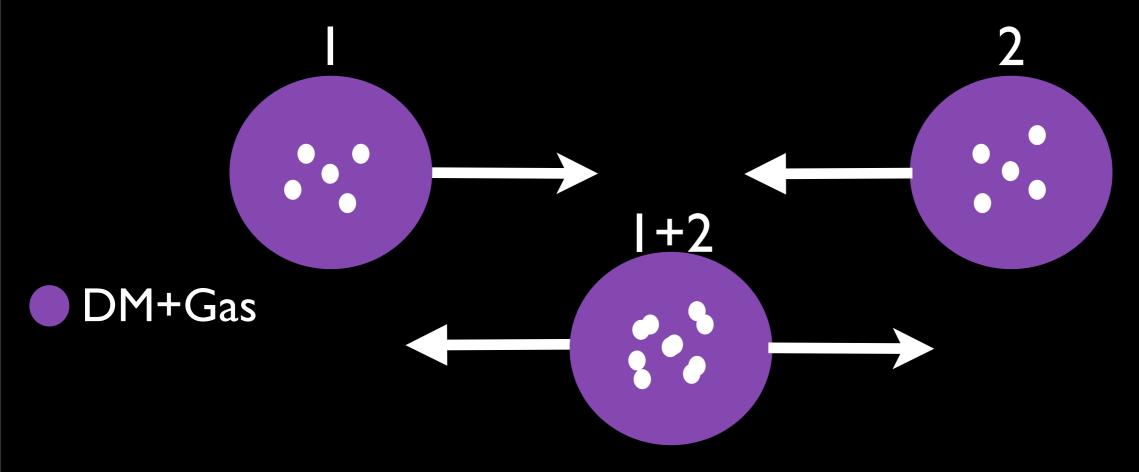


 $\sigma/m = 1 \text{ cm}^2/g$

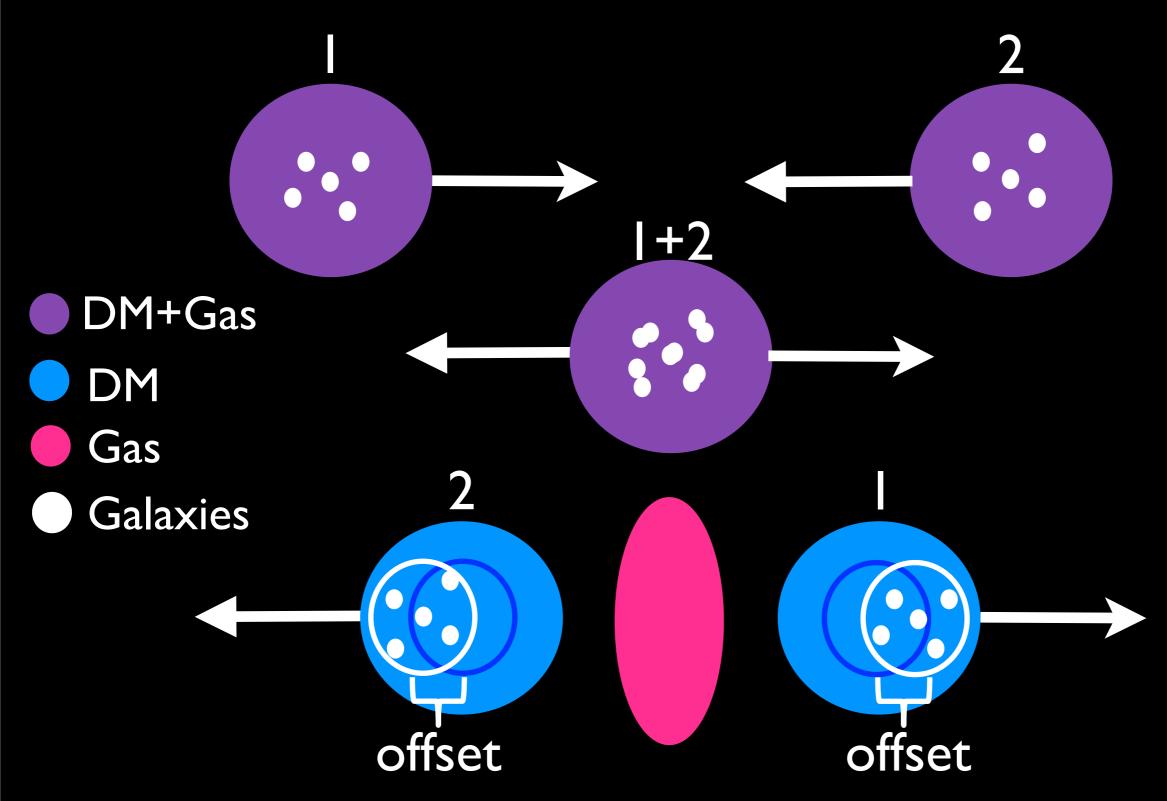
Dissosiative Clusters



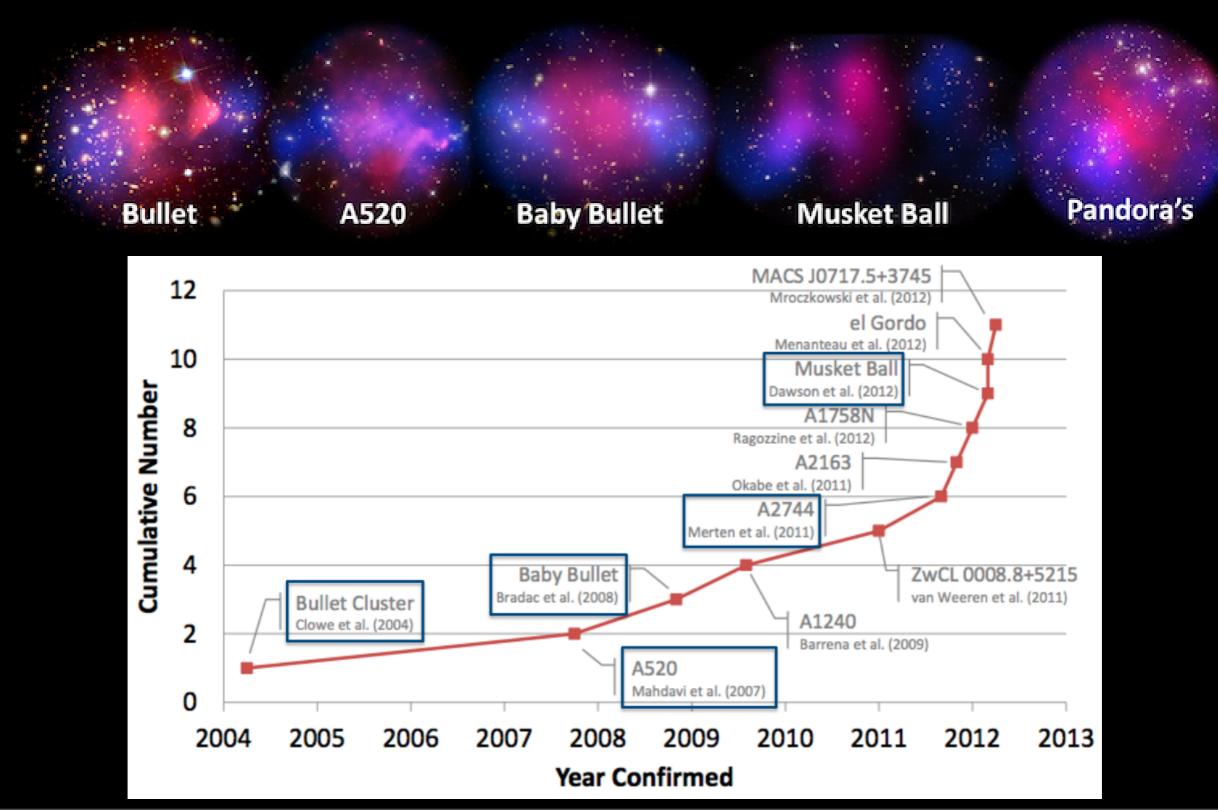
Dissosiative Clusters



Dissosiative Clusters

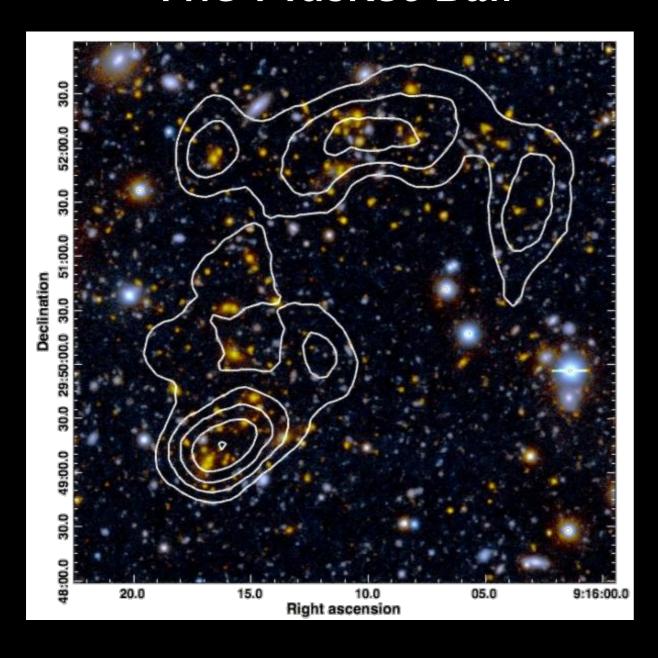


Observations



Observations

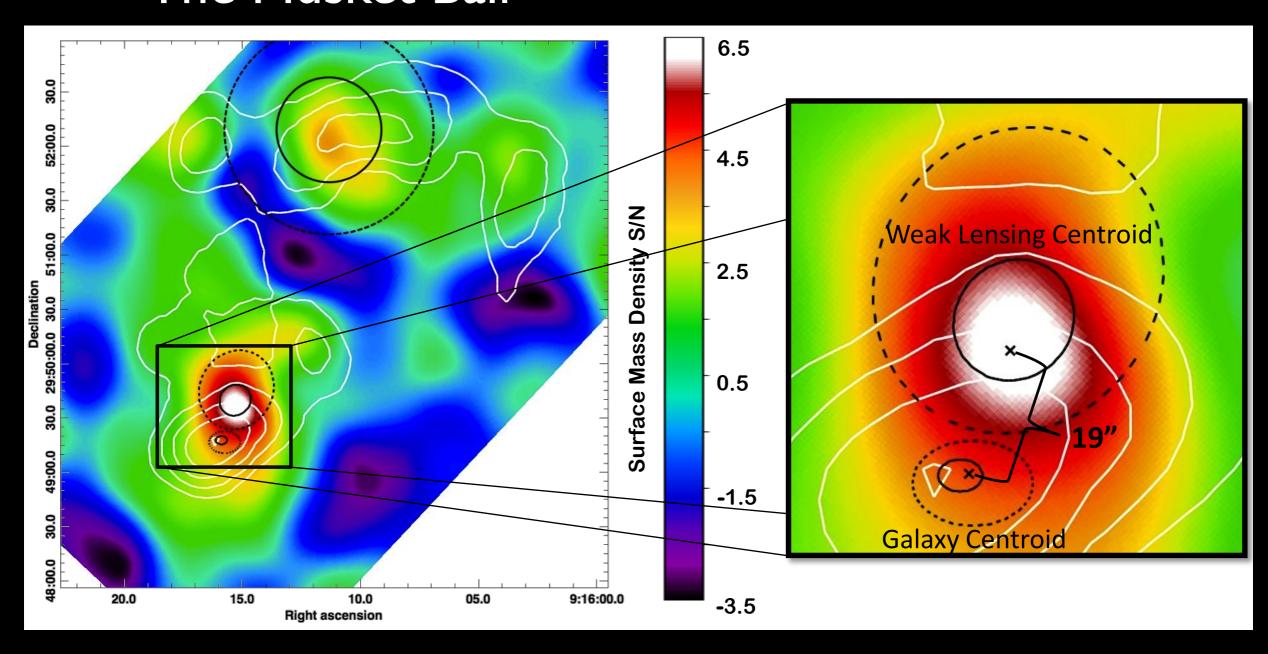
The Musket Ball



Dawson et al. 2012

Observations

The Musket Ball



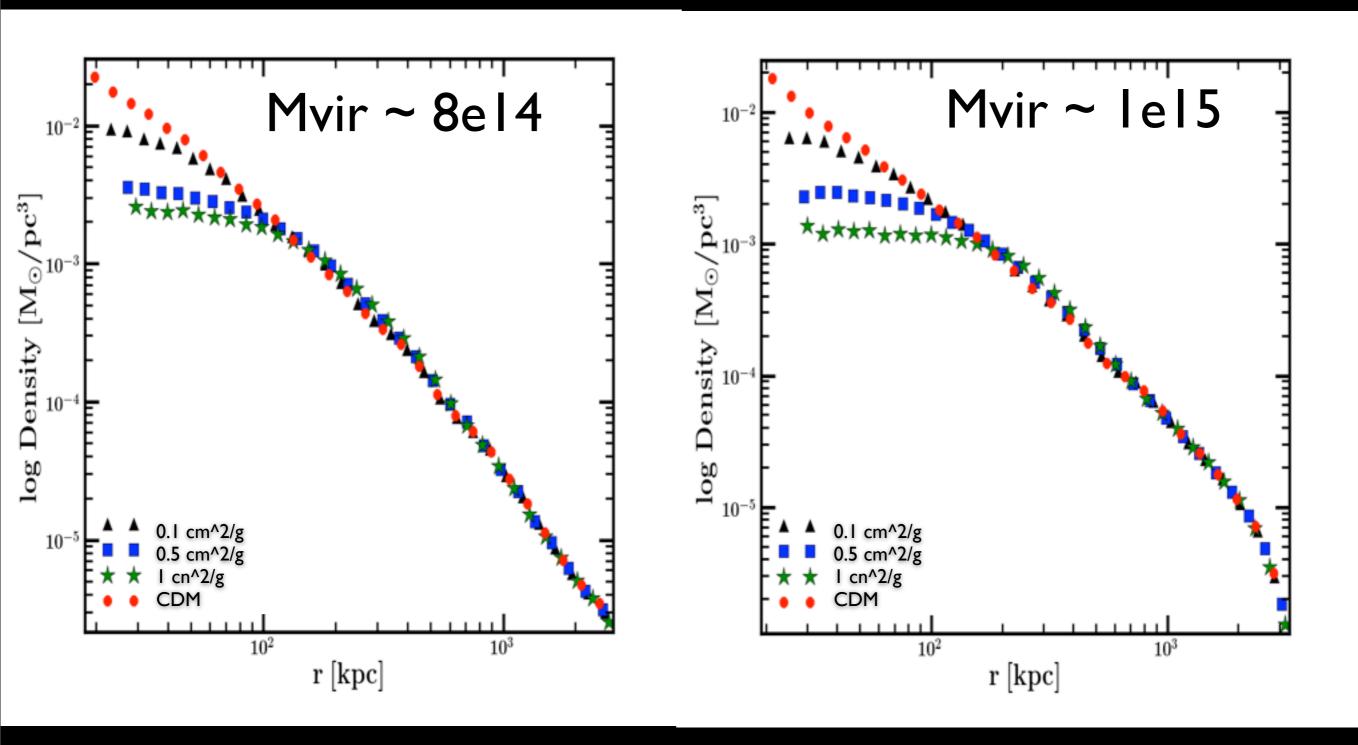
Dawson et al. 2012

Conclusions

- SIDM with $\sigma/m < 1 \text{ cm}^2/g$ is alive!
- 0.1 < σ/m < 0.5 cm²/g is the interesting regime, able to solve the cusp/core problem and TBTF while still consistent with cluster observations.
- Merging clusters are a promising way to probe the $\sigma/m > 0.1$ cm²/g regime. MCC will either yield a measurement or rule out the astrophysical interesting cross sections.

Thank You

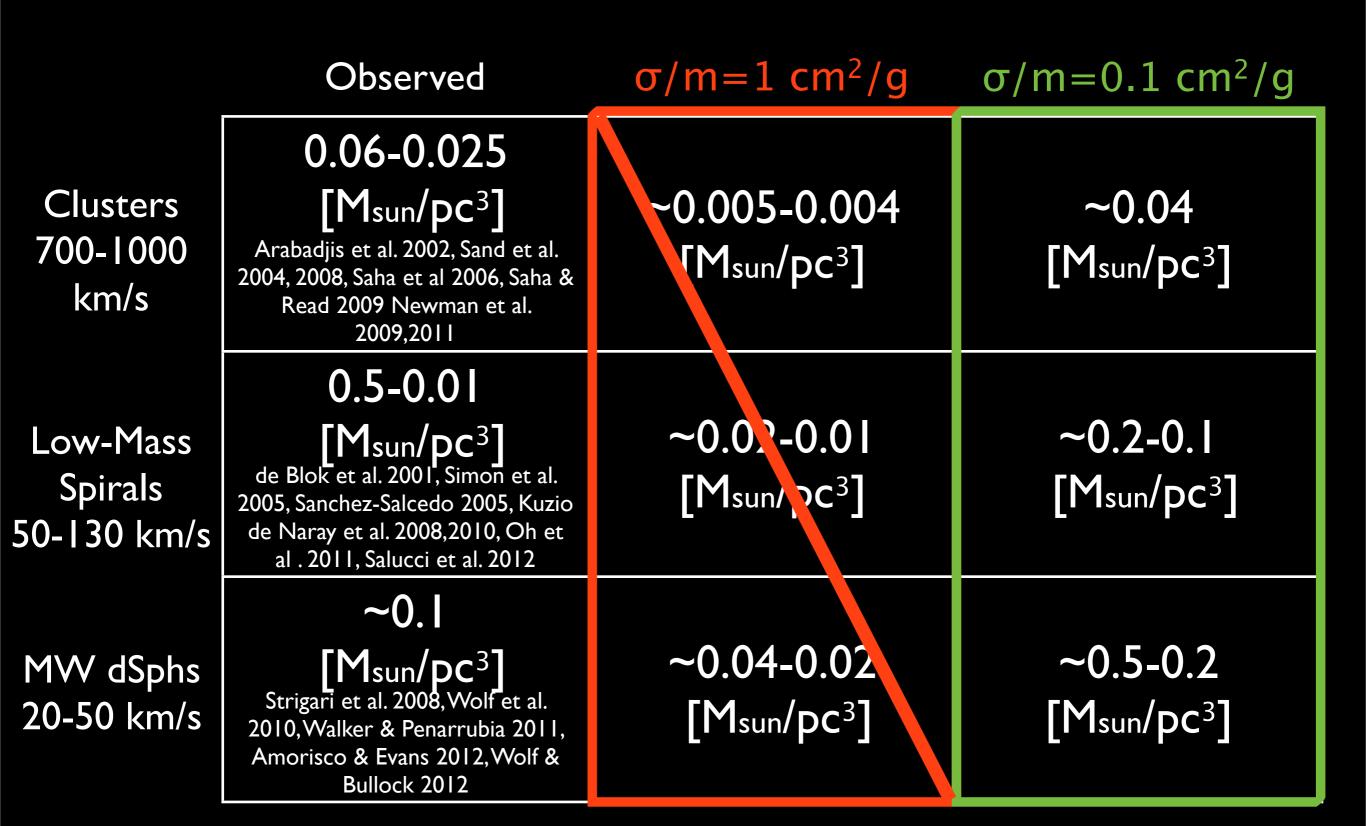
Work in progress - More simulations

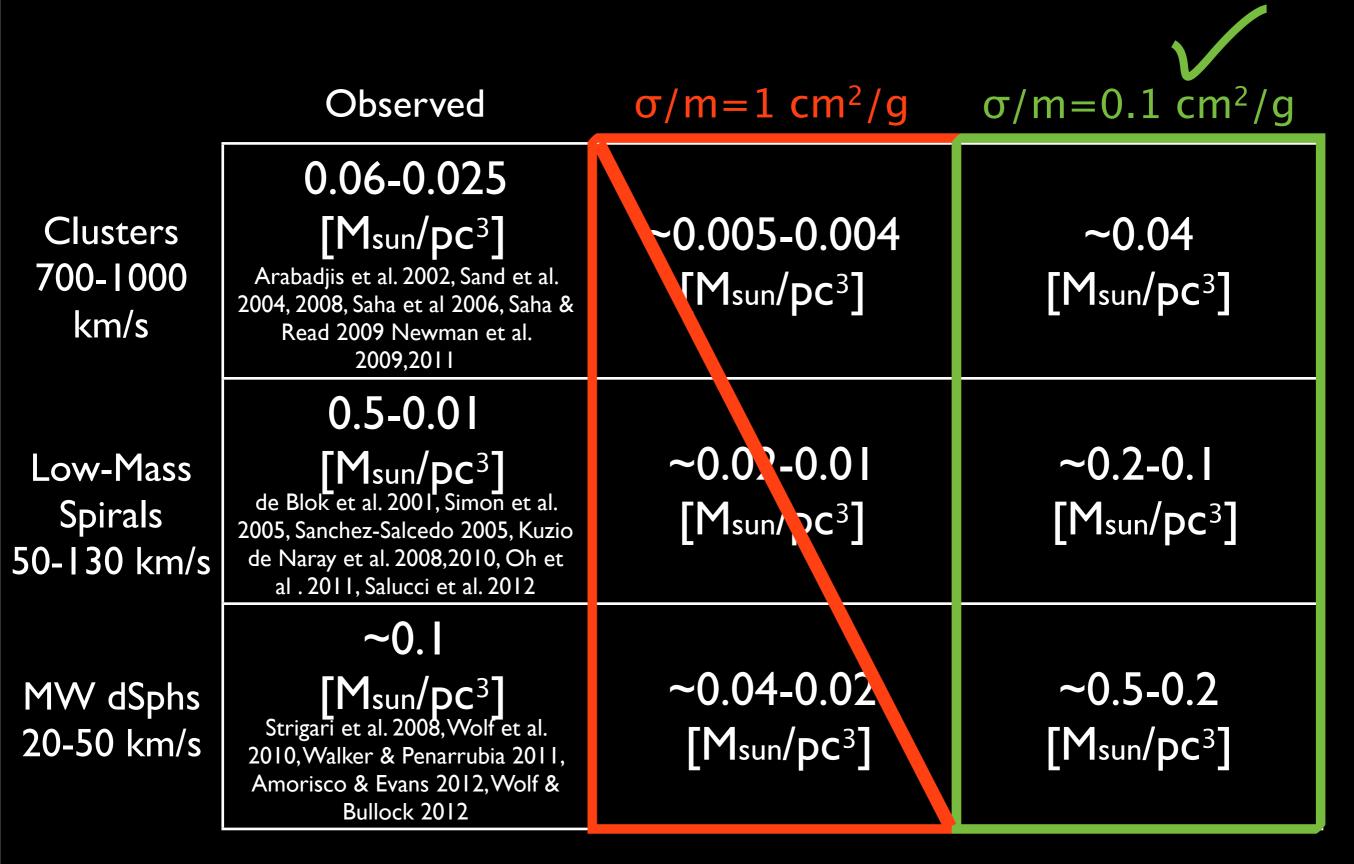


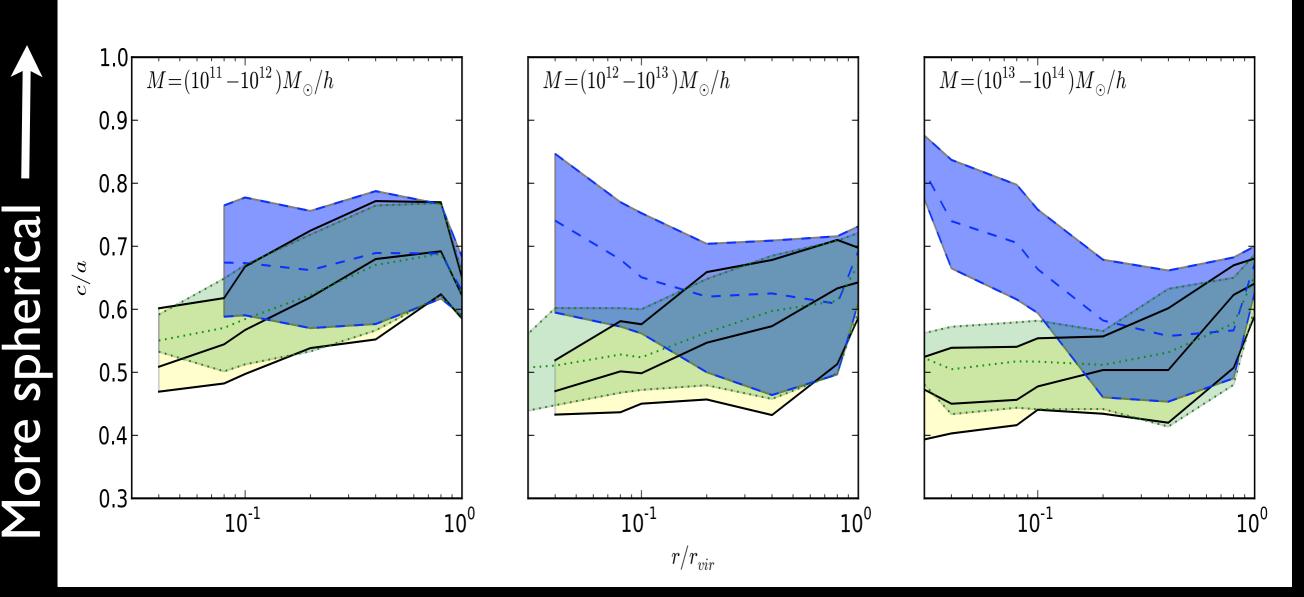
 $\sigma/m = 0.1-0.5 \text{ cm}^2/g \text{ not ruled out}$

	Observed	$\sigma/m=1$ cm ² /g	$\sigma/m=0.1 \text{ cm}^2/g$
Clusters 700-1000 km/s	0.06-0.025 [Msun/pc ³] Arabadjis et al. 2002, Sand et al. 2004, 2008, Saha et al 2006, Saha & Read 2009 Newman et al. 2009,2011	~0.005-0.004 [Msun/pc ³]	~0.04 [Msun/pc ³]
Low-Mass Spirals 50-130 km/s	O.5-0.01 [Msun/pc ³] de Blok et al. 2001, Simon et al. 2005, Sanchez-Salcedo 2005, Kuzio de Naray et al. 2008,2010, Oh et al. 2011, Salucci et al. 2012	~0.02-0.01 [Msun/pc ³]	~0.2-0.1 [Msun/pc ³]
MW dSphs 20-50 km/s	~0. I [Msun/pc ³] Strigari et al. 2008, Wolf et al. 2010, Walker & Penarrubia 2011, Amorisco & Evans 2012, Wolf & Bullock 2012	~0.04-0.02 [Msun/pc ³]	~0.5-0.2 [Msun/pc ³]

	Observed	$\sigma/m=1 \text{ cm}^2/g$	$\sigma/m=0.1 \text{ cm}^2/g$
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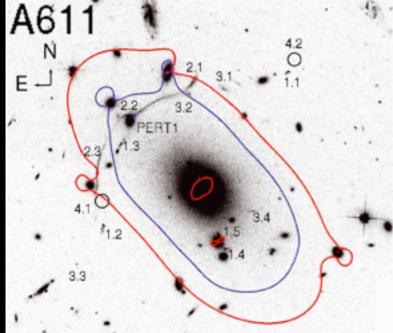






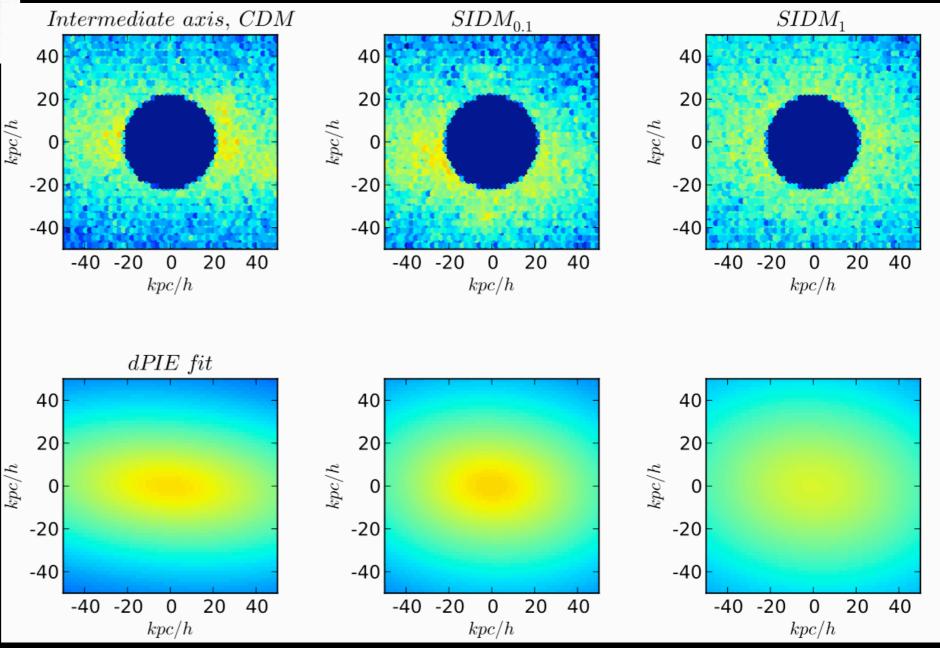
Radius/rvir

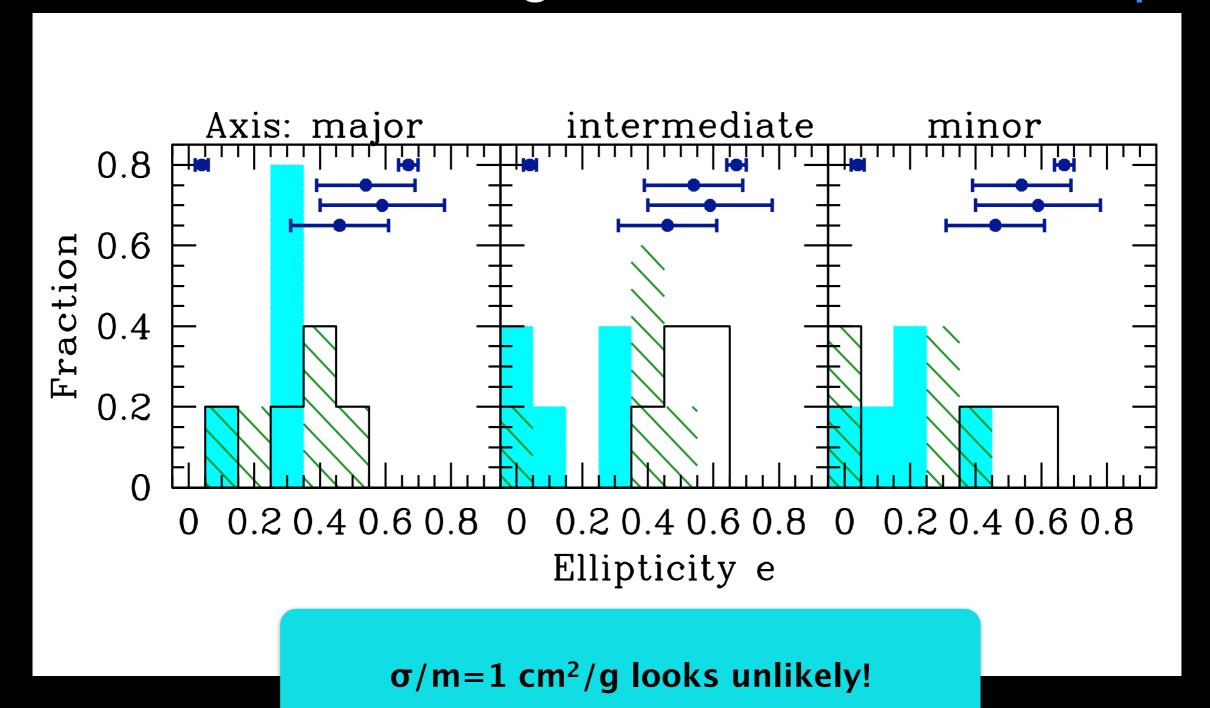
 $\sigma/m = 1 \text{ cm}^2/g$ $\sigma/m = 0.1 \text{ cm}^2/g$ collisionless



From LoCuSS sample Richard+ 2010

We see surface density (or gravitational potentials) in projection.



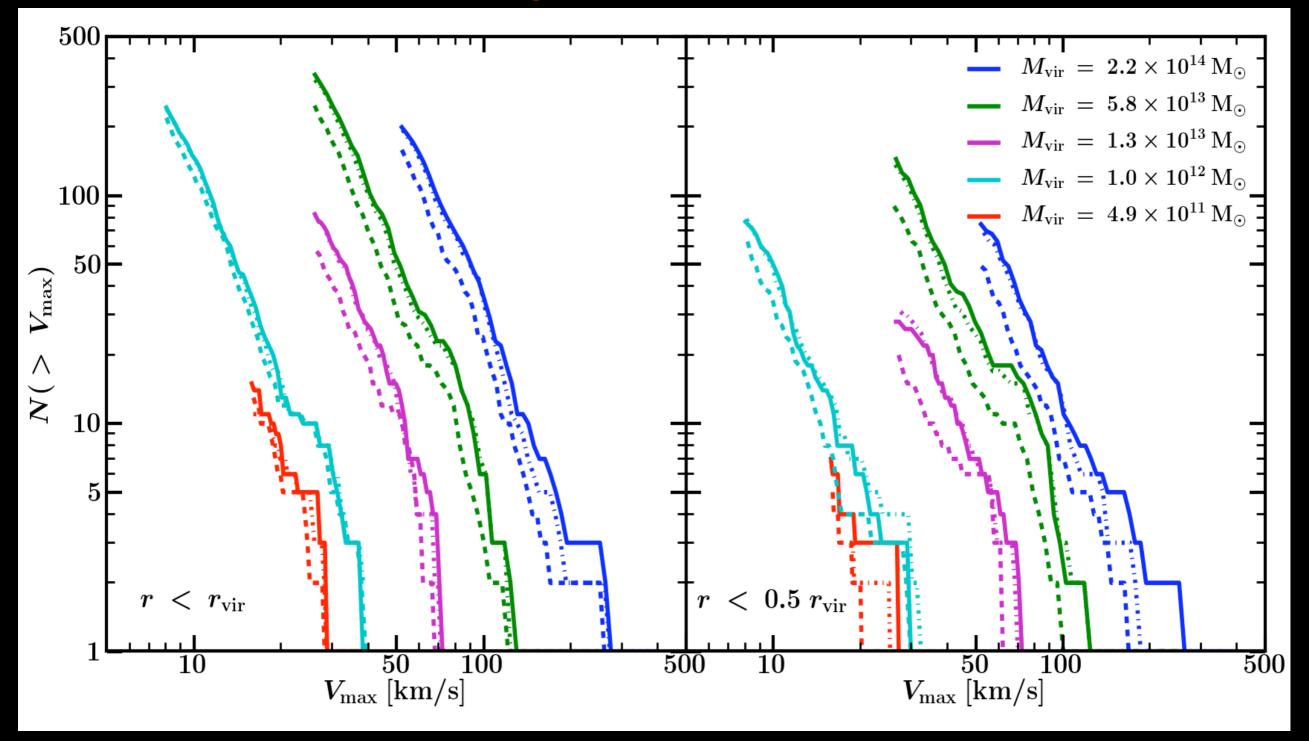


This is more than an order of magnitude less stringent than Miralda-Escude (2002), the reason is that:

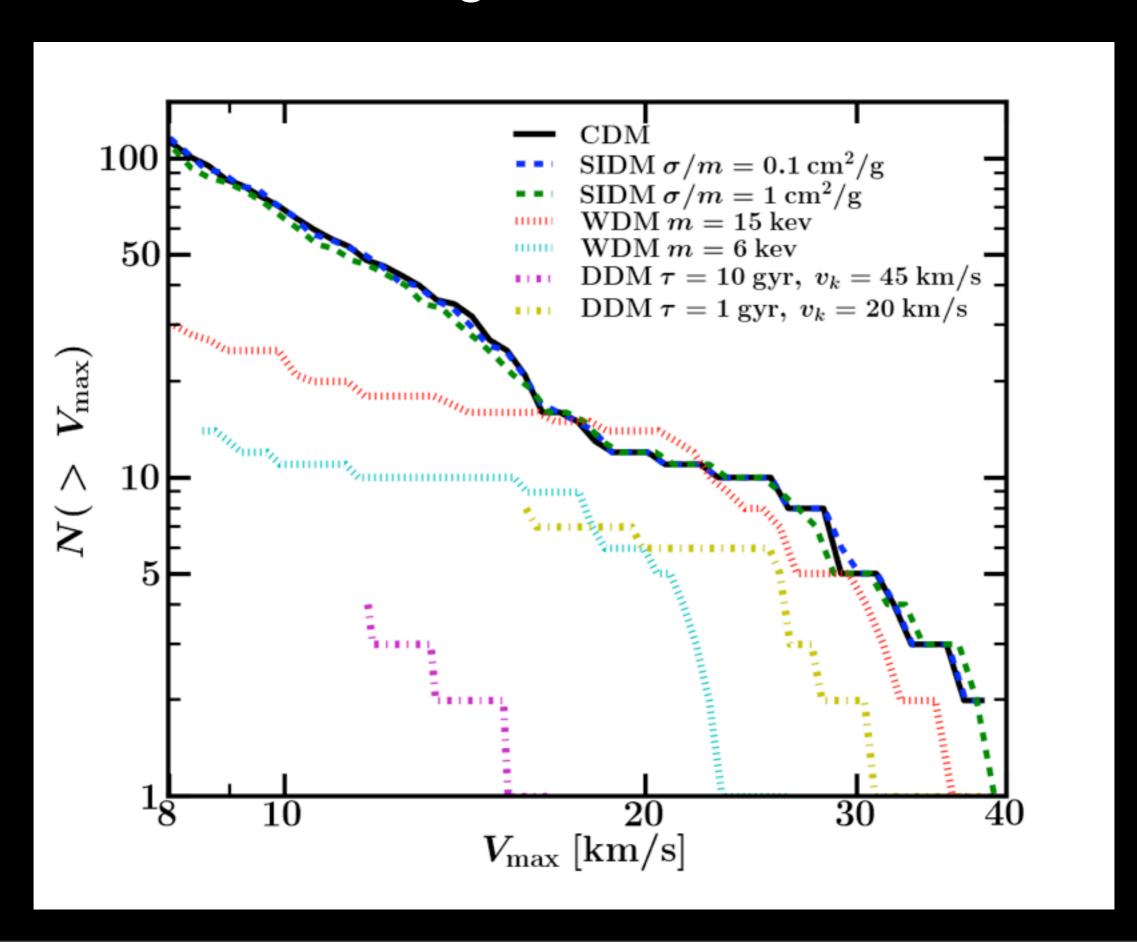
- Halos get spherical only within the cores
- If inner parts have flattened density, outer parts have even greater weight.

Results from cosmological simulations - Substructure

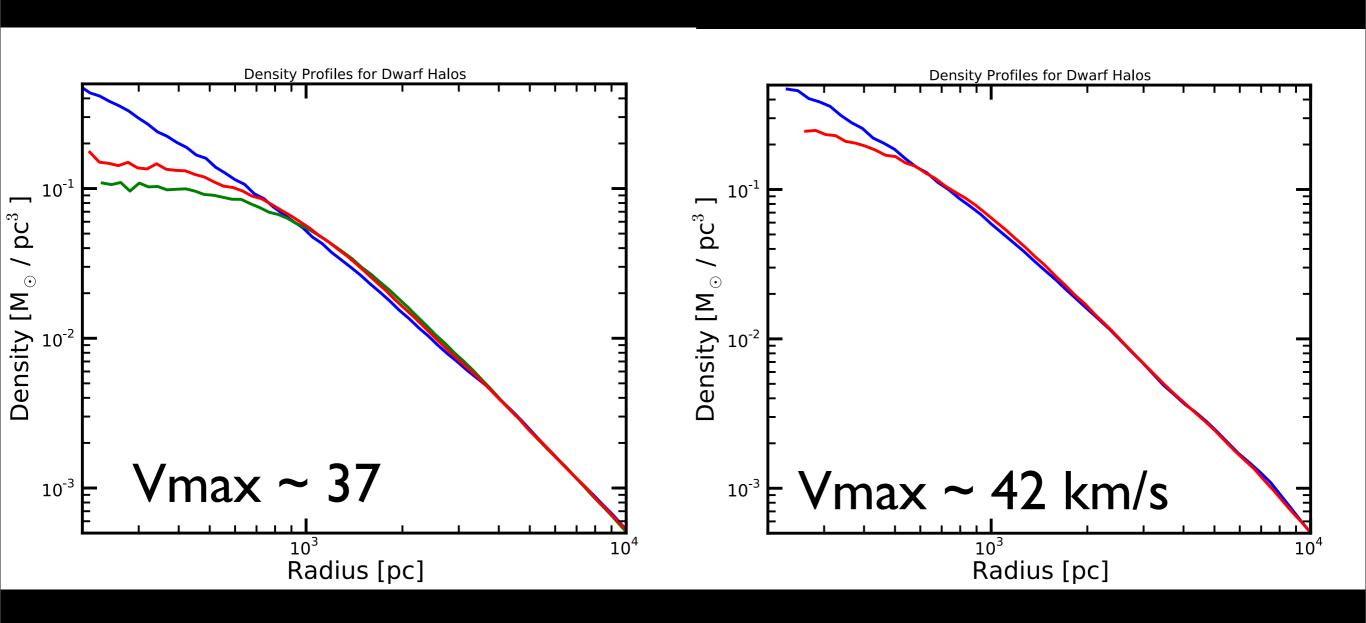
SIDM & CDM have very similar subhalo Vmax functions



Results from cosmological simulations - Substructure



Work in progress - More simulations



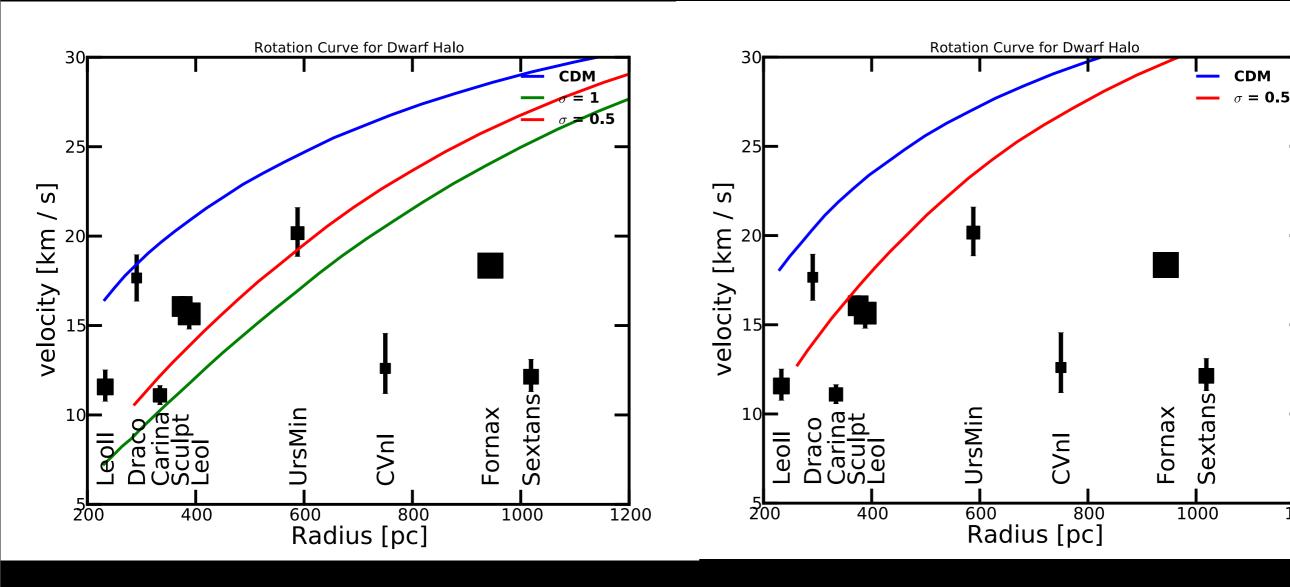
Core size of ~0.6-8 kpc and Central densities of ~0.05 Msun/pc³ for $\sigma/m = 0.5$ cm² /g

Oliver Elbert et al. in prep

Work in progress - More simulations

Vmax ~ 37 km/s

 $Vmax \sim 42 \text{ km/s}$



Consitent with the most lominous MW dwarfs

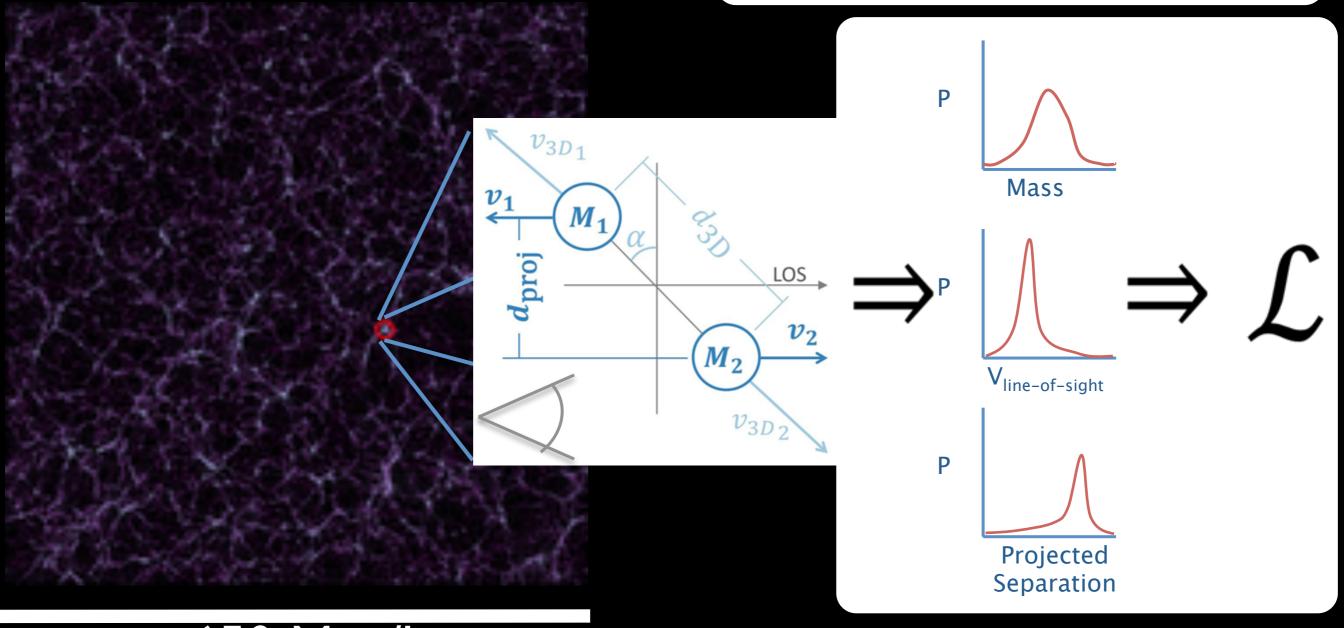
Oliver Elbert et al. in prep

1200

Predictions vs. Observations

Importance Sampling

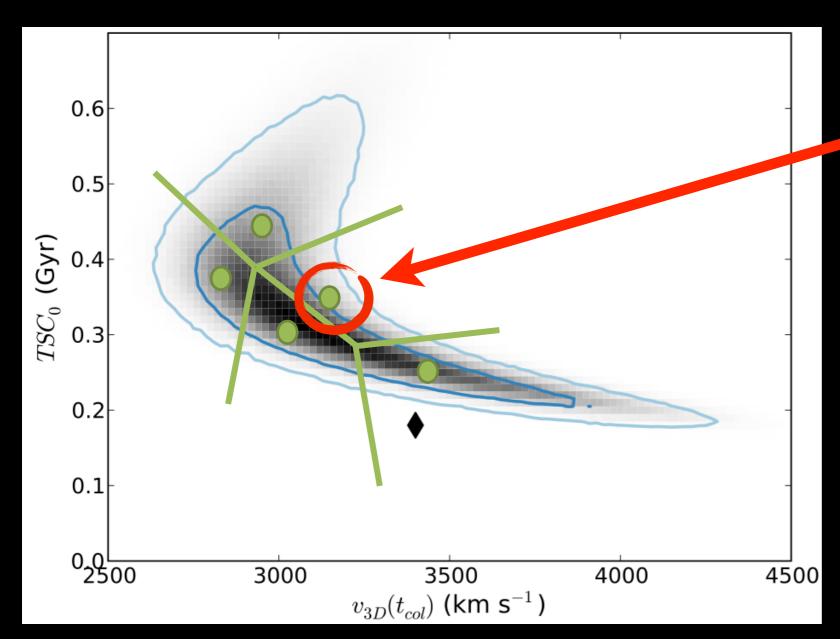




650 Mpc/h

Predictions vs. Observations



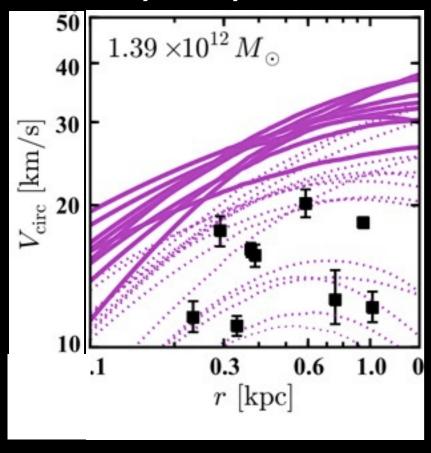


Zoom in simulations with hi-res and SIDM

MCC will either yield a measure or rule out the astrophysically interesting SIDM cross sections!!

Observations

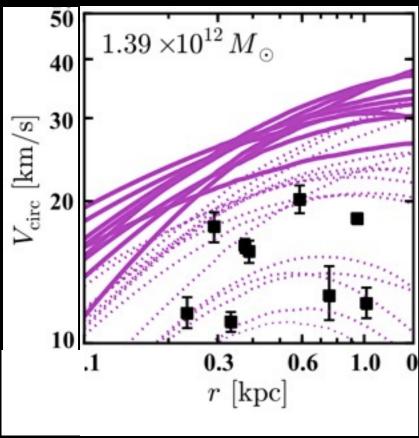
Observations Milky Way dwarfs



"**Too big to fail"** (Boylan-Kolchin+ 2011)

Need less DM in ~100 pc in 10^9 – 10^{10} M $_{\odot}$ halos Cores in ~0.5 kpc observed Walker&Penarrubia 2011

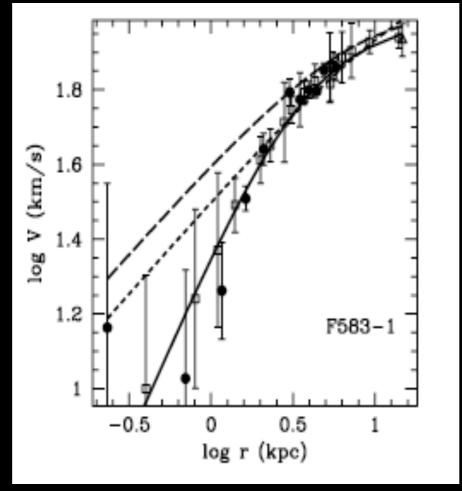
Observations Milky Way dwarfs



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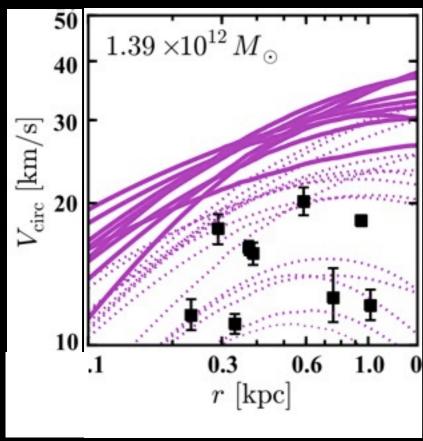
Low-mass Spirals



Dwarf core problem (Kuzio de Naray+ 2008)

Need cores in $\sim 0.5-5$ kpc in 10^{11} M $_{\odot}$ halos

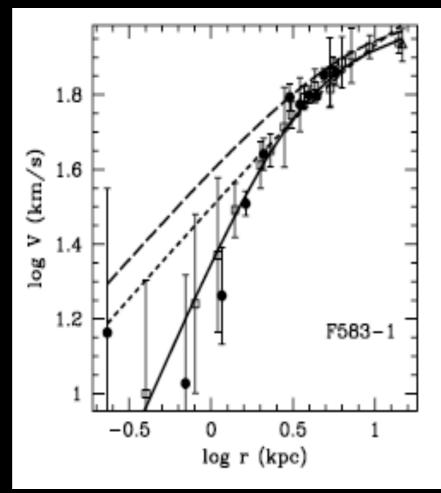
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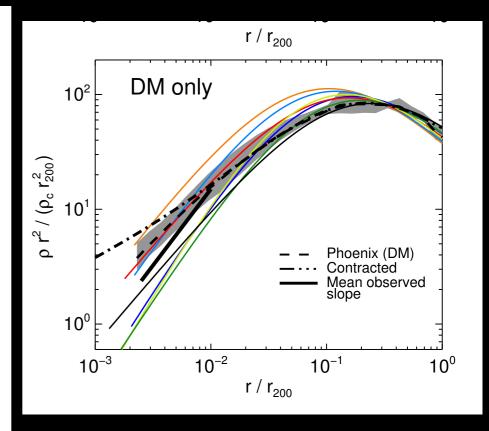
Low-mass Spirals



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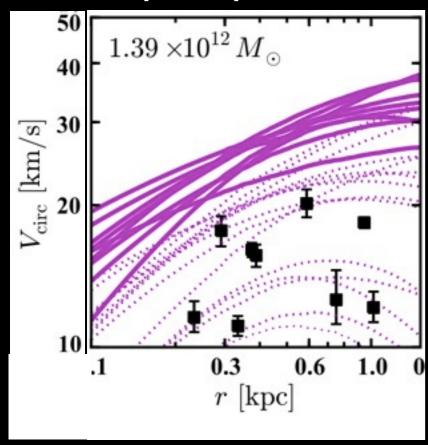


Galaxy cluster densities

ρ ~ r^{-β} Drew Newman (Newman+ 2012a,b)

Allow cores of $\sim 30 \text{ kpc}$ in $10^{15} \text{ M}_{\odot}$ halos

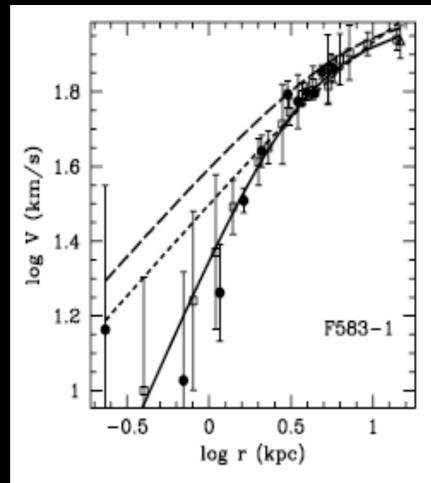
Observations Milky Way dwarfs



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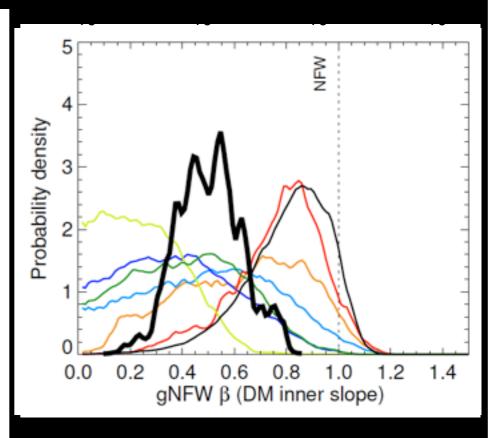
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Galaxy cluster densities

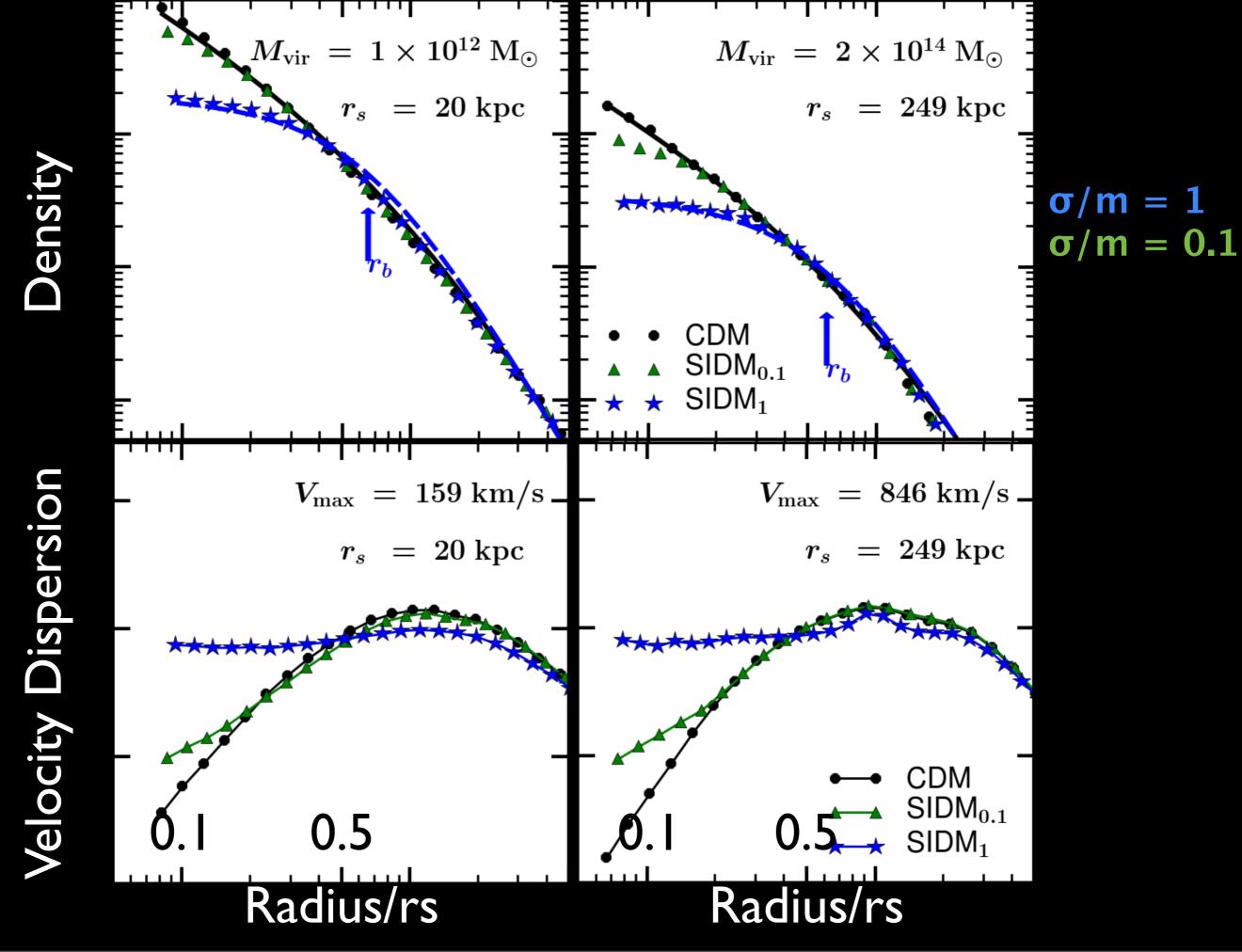
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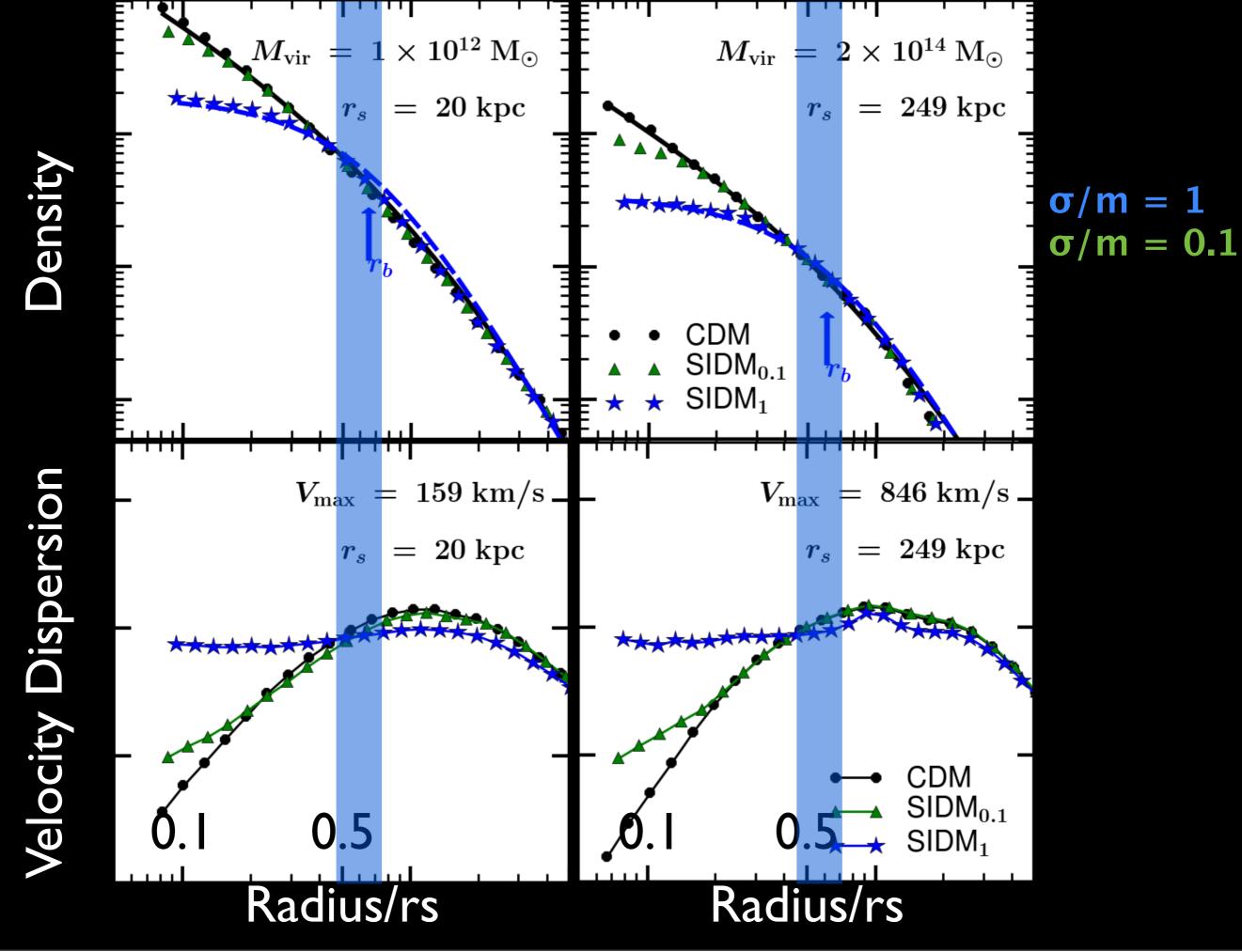
Allow cores of $\sim 30 \text{ kpc}$ in $10^{15} \text{ M}_{\odot}$ halos

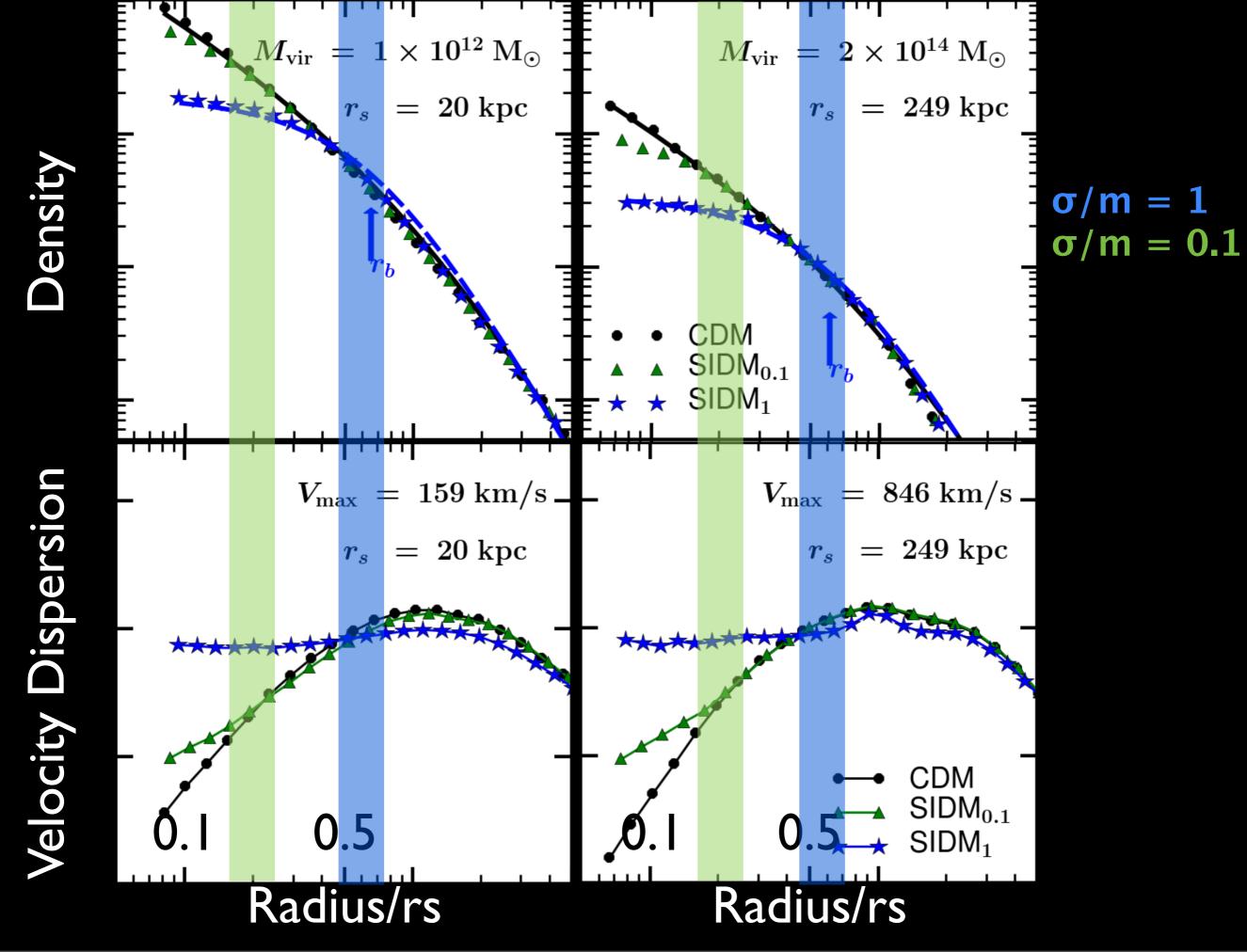
 $\sigma/m = 1$ $\sigma/m = 0.1$

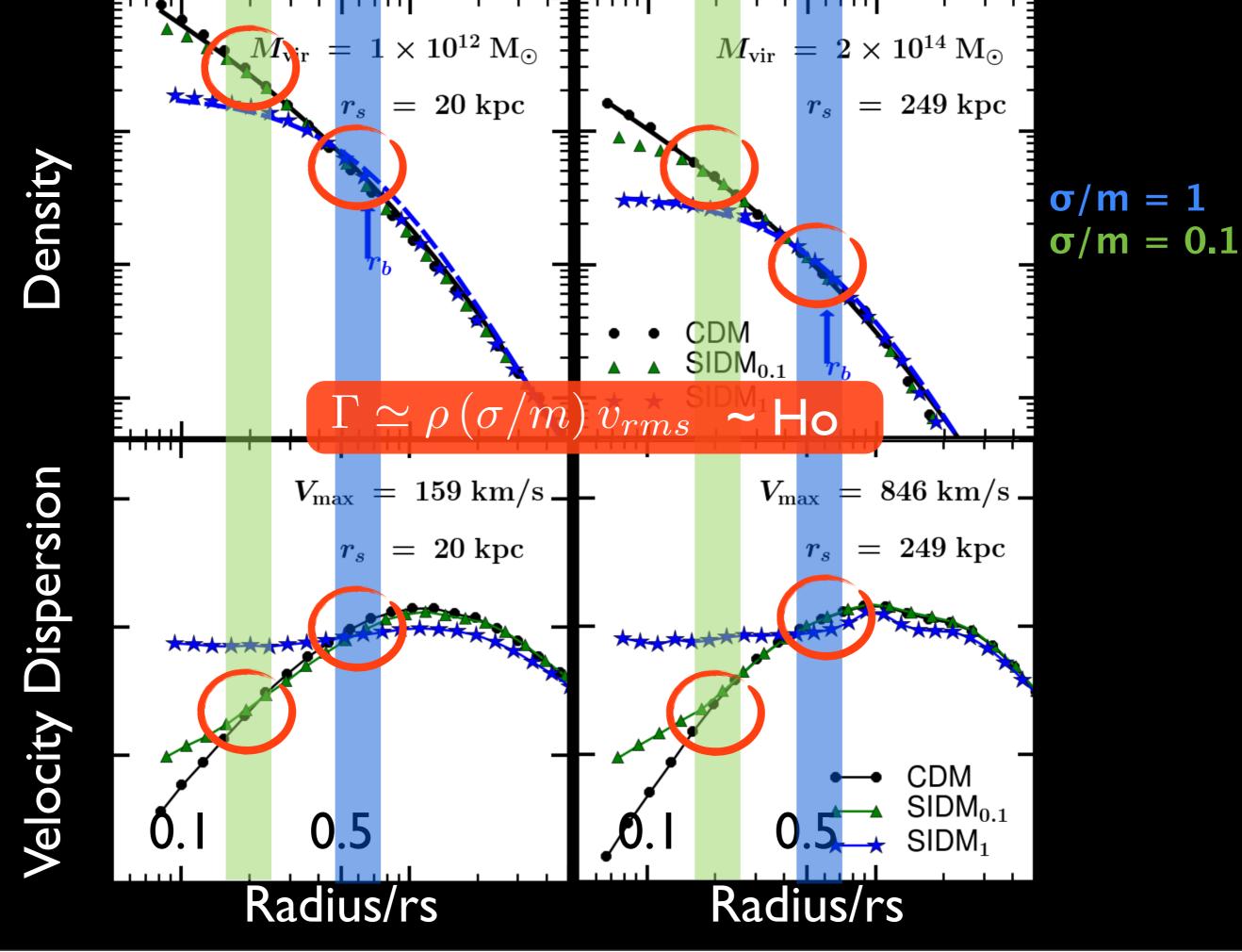
Radius/rs

Radius/rs









Previous Constraints

Reference (Constraint [cm ² /g]	From	Problem
Yoshidal et. al 2000	$\sigma/m < \sim 0.1$	Cluster density core	One cluster
Dave et. al 2001	$\sigma/m = 0.1-10$	Dwarfs density Cores	Narrow mass range
Gnedin & Ostriker 2001	$\sigma/m < 0.3$	Subhalo evaporation	Overestimated subhalo evaporation
Miralda-Escude 2002	$\sigma/m < 0.02$	Halo shapes	Overestimated halo sphericity
Randall et al. 2008	σ/m < 0.7–1.25	Bullet Cluster	High central densities and relative vel.

Previous Constraints

Constraint [cm²/g]

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Ostriker 2001	U/III \ U.J	evaporation	evaporation
Miralda-Escude	-1		Overestimated
2002	0/111 \ 0.02	i iaio siiapes	halo sphericity
Randall et al. 2008	σ/m < 0.7–1.25	Bullet Cluster	High central densities and relative vel.

Today's Constraints

Reference Constraint [cm²/g] From Problem

Rocha et. al 2012 Peter et. al 2012	σ/m~0.1-0.5	cores & shapes	extrapolations
Dave et. al 2001	$\sigma/m = 0.1-10$	Dwarfs cores	Narrow mass range
Randall et al. 2008	$\sigma/m < 0.7-1.25$	Bullet Cluster	High central densities and relative vel.
Vogelsberger et al.2012 Zavala et al. 2012	σ/m > 0.1 Velocity dependence may be needed	MW dwarfs solves TBTF	MW dwarfs only (resolution?)
MCC	Expect best constraints stay tuned!!	Merging Clusters	Time will tell

Today's Constraints

From

Problem

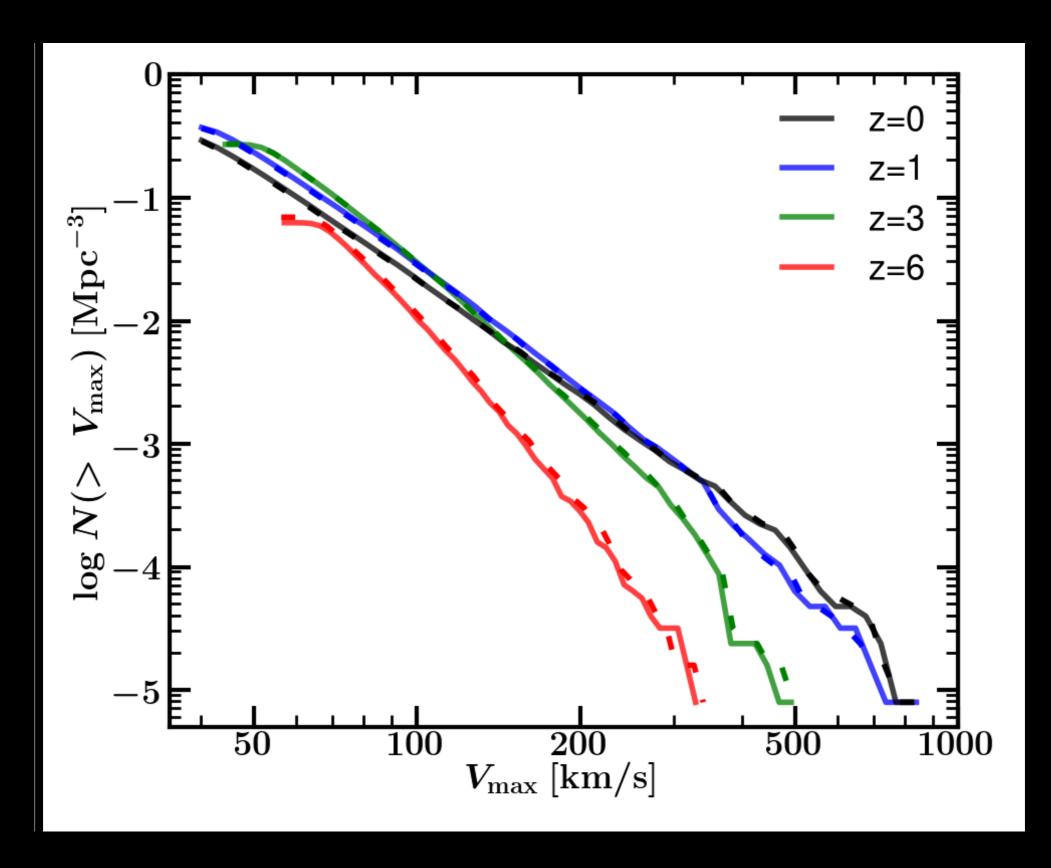
Constraint [cm²/g]

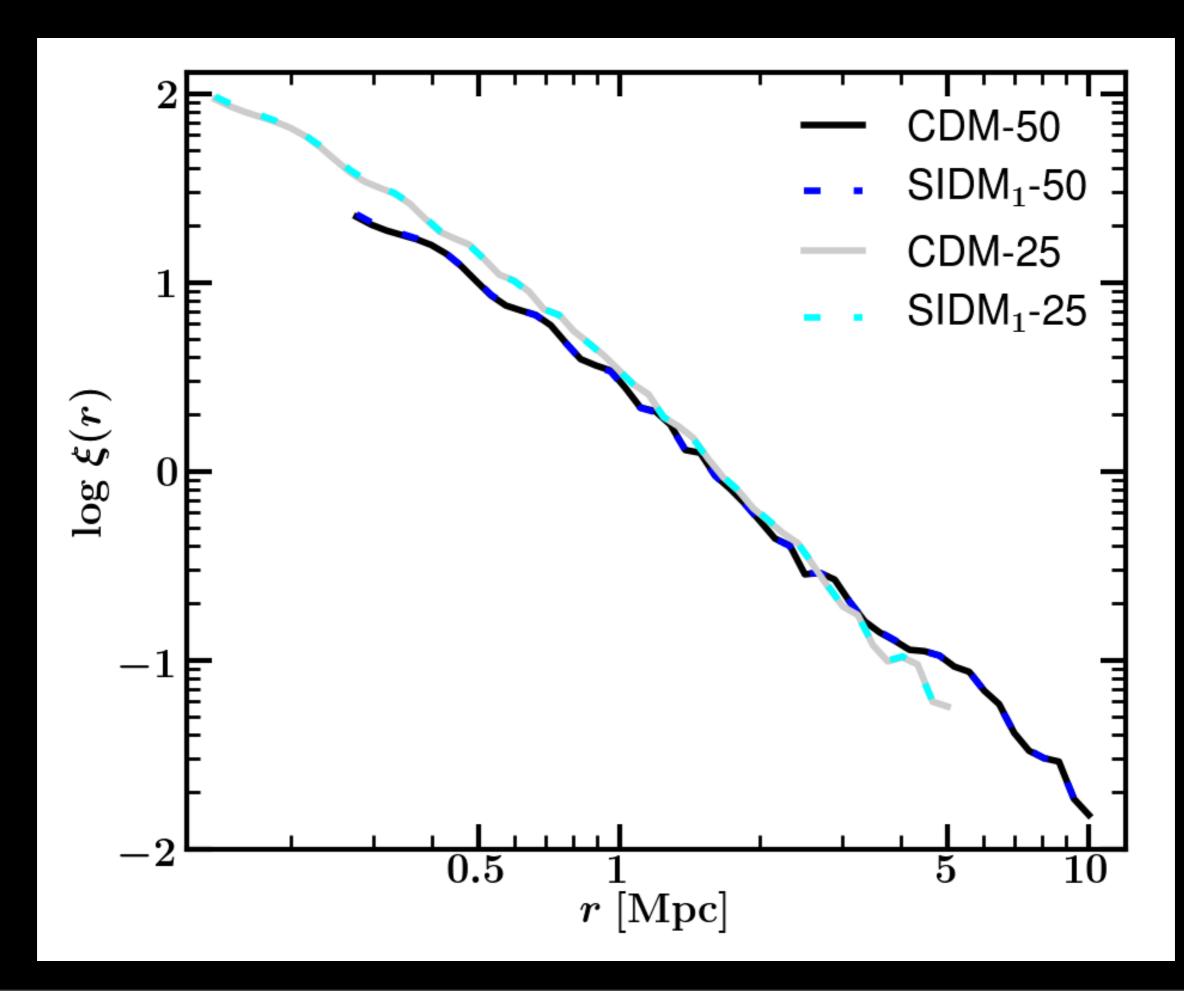
			TTODICITI
Rocha et. al 2012 Peter et. al 2012	σ/m~0.1–0.5	cores & shapes	extrapolations
Dave et. al 2001	$\sigma/m = 0.1-1.0$	Dwarfs cores	Narrow mass range
Randall et al. 2008	$\sigma/m < 0.7-1.25$	Bullet Cluster	High central densities and relative vel.
Vogelsberger et al.2012 Zavala et al. 2012	σ/m > 0.1 Velocity dependence may be needed	MW dwarfs solves TBTF	MW dwarfs only (resolution?)
MCC	Expect best constraints stay tuned!!	Merging Clusters	Time will tell

For Gev particles these are equivalent to strong force interactions (nucleon-nucleon scattering)!!

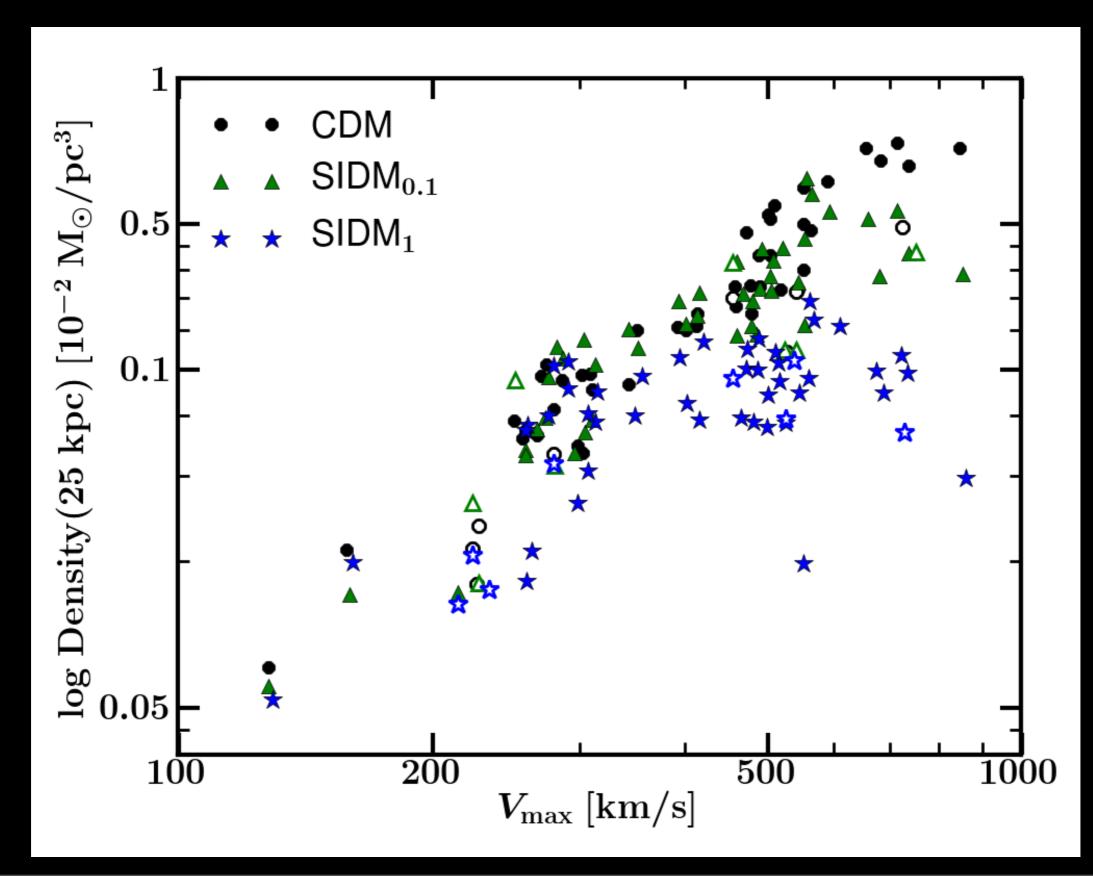
Reference

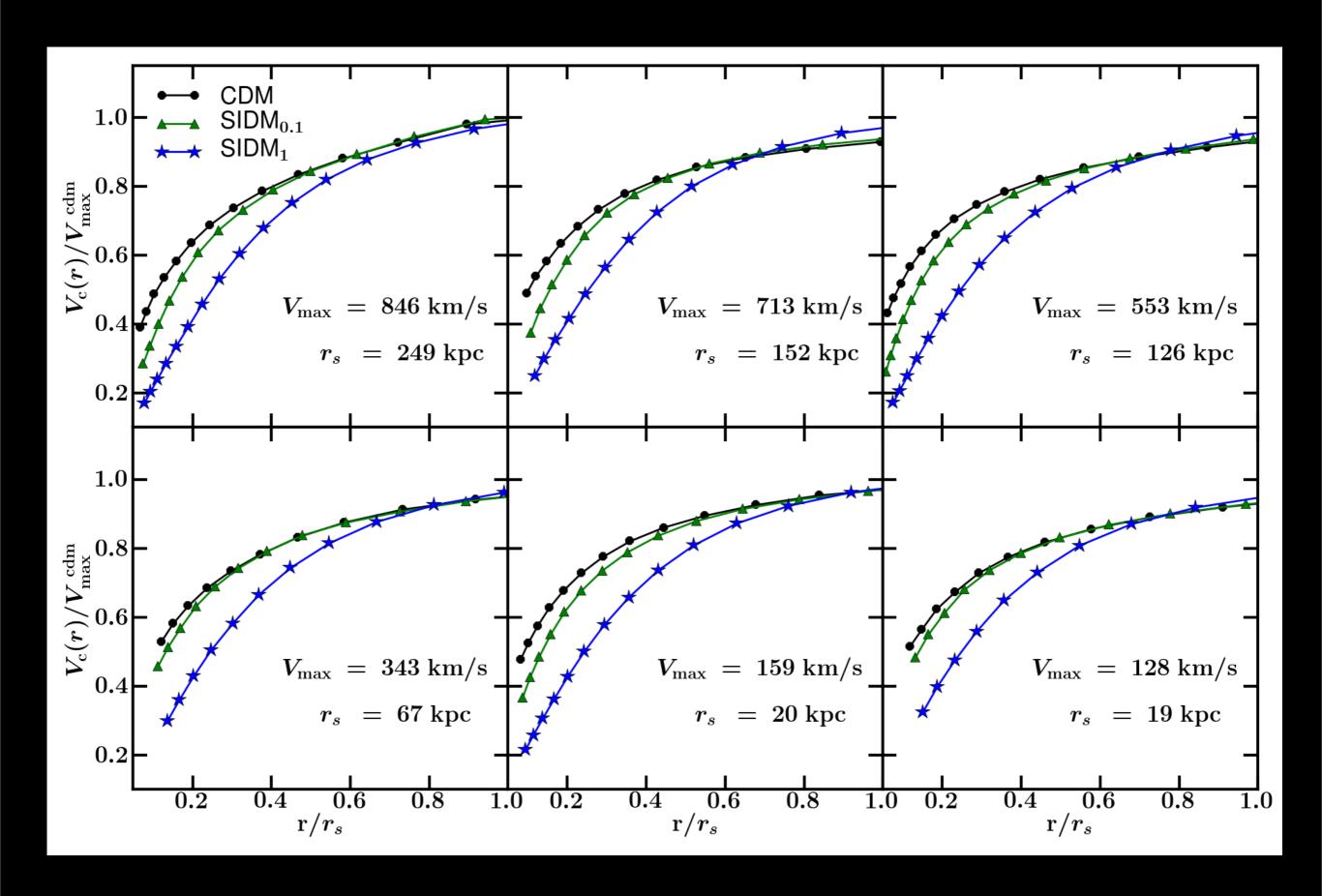
Identical Abundance of Halos

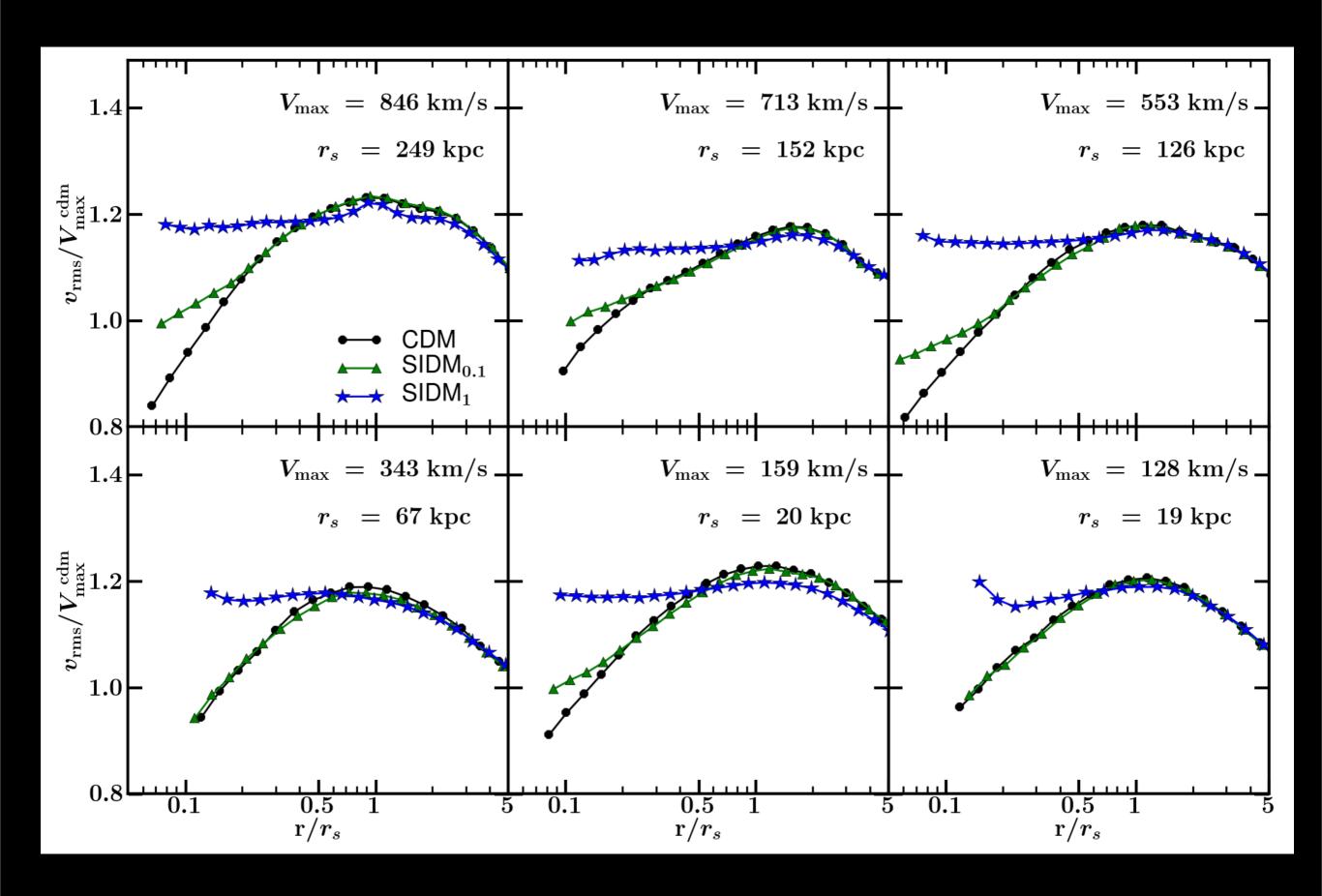


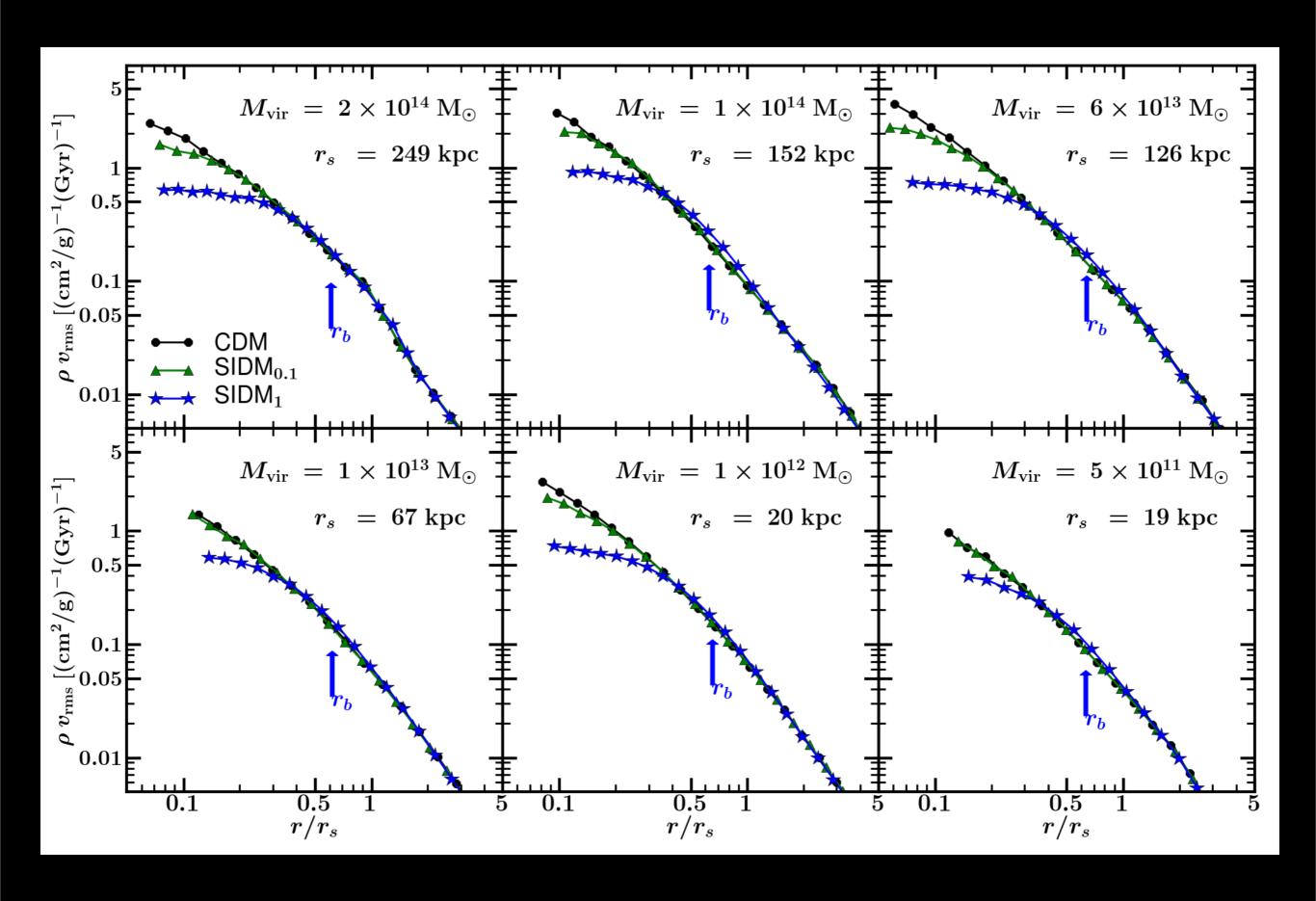


Reduced Central Densities









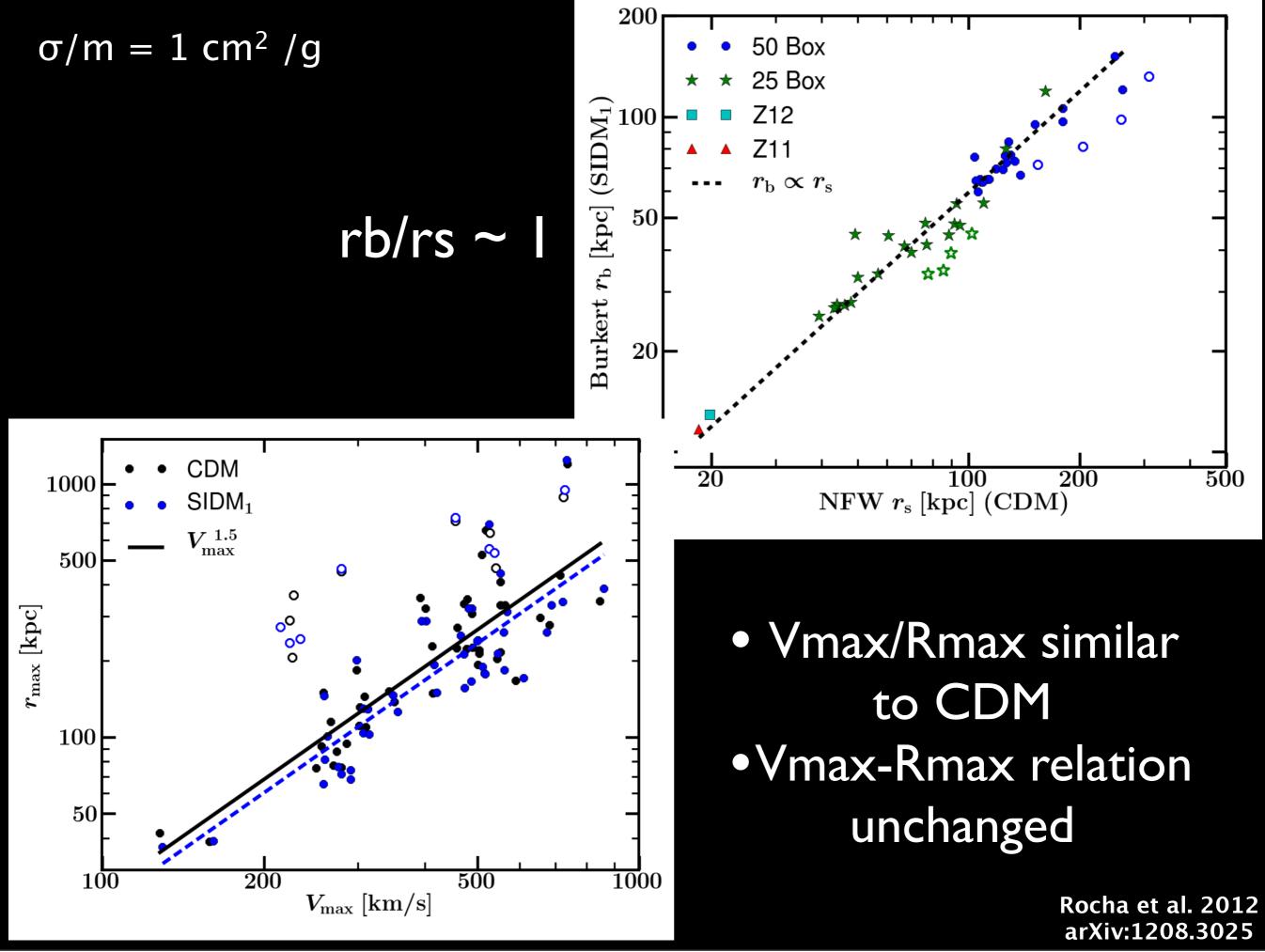


Table 1: Simulations discussed in this paper.						
Name	Volume	Number of Particles	Particle Mass	Force Softening	Smoothing Length	Cross-section
	$L_{\rm Box} [h^{-1} {\rm Mpc}]$	$N_{ m p}$	$m_{\rm p} [h^{-1} \mathrm{M}_{\odot}]$	$\epsilon [h^{-1} \mathrm{kpc}]$	$h_{\rm si} [h^{-1} {\rm kpc}]$	$\sigma/m [\mathrm{cm}^2/\mathrm{g}]$
CDM-50	50	512^{3}	6.88×10^{7}	1.0	_	0
CDM-25	25	512^{3}	8.59×10^{6}	0.4	_	0
CDM-Z11	$(3R_{\rm vir})^*$	2.5×10^{6} *	1.07×10^{6} *	0.3	_	0
CDM-Z12	$(3R_{\rm vir})^*$	5.6×10^{7} *	$1.34 \times 10^{5*}$	0.1	_	0
SIDM _{0.1} -50	50	512^{3}	6.88×10^{7}	1.0	2.8ϵ	0.1
$SIDM_{0.1}$ -25	25	512^{3}	8.59×10^{6}	0.4	$2.8~\epsilon$	0.1
$SIDM_{0.1}$ -Z11	$(3R_{ m vir})^*$	$2.5 \times 10^6 *$	1.07×10^{6} *	0.3	$2.8~\epsilon$	0.1
$SIDM_{0.1}$ -Z12	$(3R_{ m vir})^*$	5.6×10^{7} *	1.34×10^{5} *	0.1	1.4ϵ	0.1
SIDM ₁ -50	50	512^{3}	6.88×10^{7}	1.0	2.8ϵ	1
$SIDM_1-25$	25	512^{3}	8.59×10^{6}	0.4	$2.8 \ \epsilon$	1
$SIDM_1$ -Z11	$(3R_{ m vir})^*$	$2.5 \times 10^6 *$	1.07×10^{6} *	0.3	$2.8 \ \epsilon$	1
SIDM ₁ -Z12	$(3R_{\rm vir})^*$	5.6×10^{7} *	$1.34 \times 10^{5*}$	0.1	$1.4~\epsilon$	1

hs	2 KY	Ve	d
US	CI Y	V C	U

$$\sigma/m=1$$
 cm²/g

 $\sigma/m=0.1 \text{ cm}^2/g$

Clus	ters
700-	1000
km	n/s

10-75 kpc

Arabadjis et al. 2002, Sand et al. 2004, 2008, Saha et al 2006, Saha & Read 2009 Newman et al. 2009,2011

95-155 kpc

16-20 kpc

Low-Mass
Spirals
50-130 km/s

0.5-8 kpc

de Blok et al. 2001, Simon et al. 2005, Sanchez-Salcedo 2005, Kuzio de Naray et al. 2008,2010, Oh et al. 2011, Salucci et al. 2012

3-10 kpc

0.6-2.5 kpc

MW dSphs 20-50 km/s

0.2-1 kpc

Walker & Penarrubia 2011

0.9-3 kpc

0	$bs\epsilon$	erv	ed

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Observed

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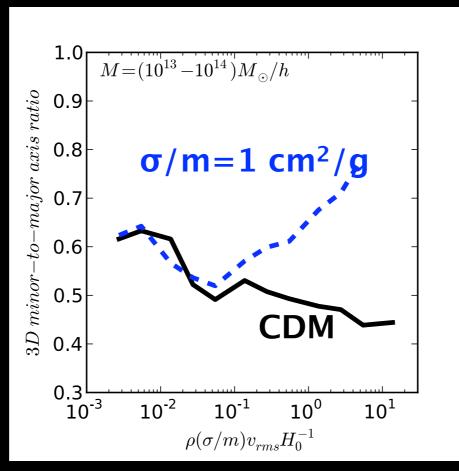
0.6-2.5 kpc

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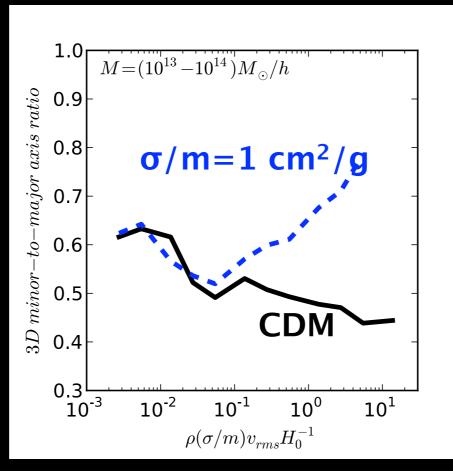
0.2-1 kpc

Walker & Penarrubia 2011

0.9-3 kpc

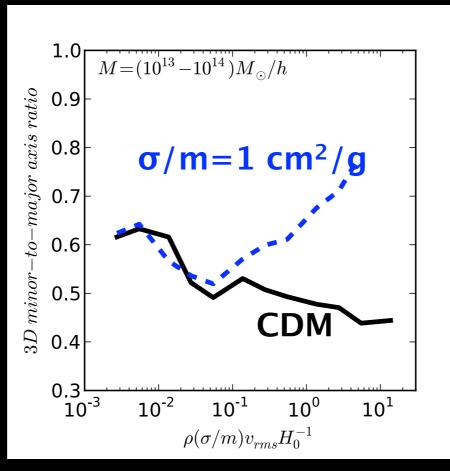


- We see surface density (or gravitational potentials) in projection.
- If inner parts have flattened density, outer parts have even greater weight.



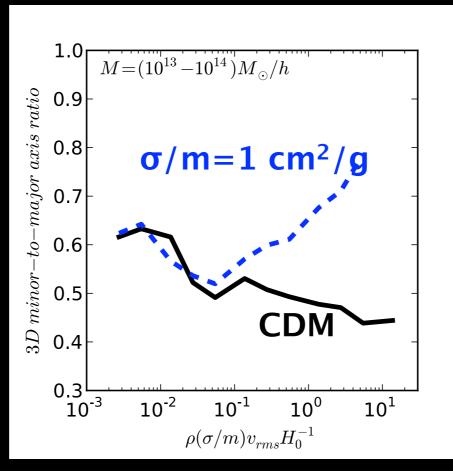
$$\Gamma/H_0 \gg 10$$

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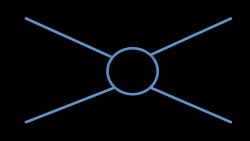
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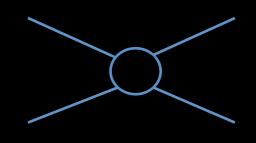


$$\Gamma/H_0 \gg 10$$

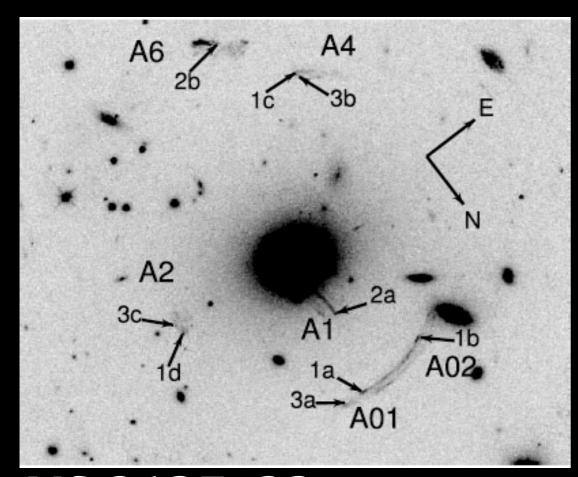
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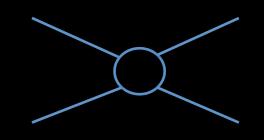
Miralda-Escude (2002)



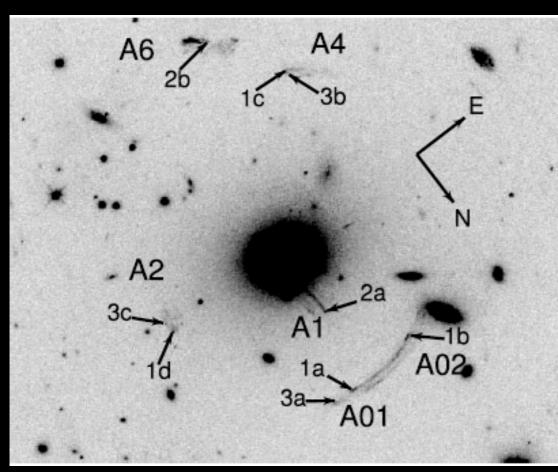
Miralda-Escude (2002)



MS 2137-23
Sand et al. 2008



Miralda-Escude (2002)

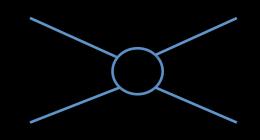


MS 2137-23 Sand et al. 2008

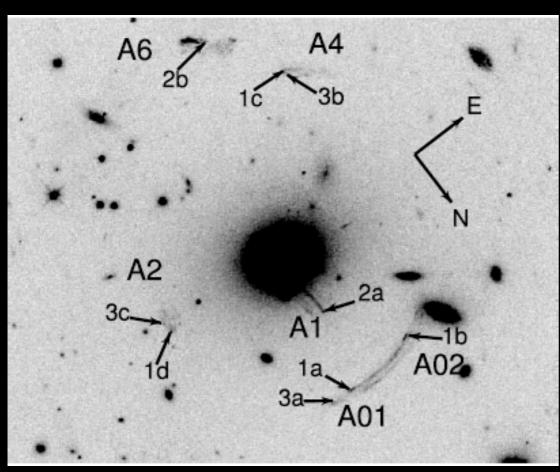
Requires a non-circularlysymmetric surface density at r > 70 kpc.

Assume $\epsilon = 0$ if $H_0 \gtrsim 1$.

 \rightarrow $\sigma/m < 0.02 cm^2/g$.



Miralda-Escude (2002)



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MS 2137-23
Sand et al. 2008

Tightest constraint by far (by > 10x)!

Constraints from: substructure

Observations

